# De Bruijn Graphs for DNA Sequencing (Part 2) ${ }^{1}$ 

Course "Discrete Biological Models" (Modelli Biologici Discreti)

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[^0]Solution: Use Euler cycle/path approach

Solution:
Use Euler cycle/path in de Bruijn graph approach instead of finding heaviest Hamiltonian cycle/path in overlap graph.

Finding an Euler cycle (or Euler path) can be solved in polynomial time.

But:
We have to find a way of modelling our problem in the right way.

Sanger sequencing vs. short read sequencing

## NGS

Next generation sequencing technologies (Illumina, 454, SOLiD, ...) generate a much larger number of reads

- high-throughput: fast acquisition, low cost
- lower quality (more errors)
- short reads (Illumina: typically $60-100 \mathrm{bp}$ )
- much higher number of reads

While overlap graph approach (with many additional details and modifications!) worked for Sanger type sequences, it no longer works for NGS data. Reason: Input too large, no efficient (= polynomial time in input size) algorithms known, since all problem variants NP-hard.

Modelling our problem with de Bruijn graphs

## N.B.

For simplicity, for now our sequence to be reconstructed is assumed to be circular. E.g. bacterial genomes are circular.


String can be read as: ATGGCGTGCA, TGGCGTGCAA, GGCGTGCAAT, ...

Definition of de Bruijn graphs
Let $\Sigma$ be our alphabet.
(E.g. $\Sigma=\{\mathrm{A}, \mathrm{C}, \mathrm{G}, \mathrm{T}\}$ or $\Sigma=\{0,1\}$ or $\Sigma=\{\mathrm{a}, \mathrm{b}, \mathrm{c}\}$ )

Definition
A digraph $G=(V, E)$ is called a de Bruijn graph of order $k$ if $V \subseteq \Sigma^{k-1}$ and for all $u, v \in V$ : if $(u, v) \in E$ then there exists a word $w \in \Sigma^{k}$ s.t. $u$ is the $(k-1)$-length prefix of $w$ and $v$ is the $(k-1)$-length suffix of $w$.

Example
$u=\mathrm{GCA}, v=\mathrm{CAA}, w=\mathrm{GCAA}$.
Note that this graph can have loops, e.g. if $u=$ AAA, then $(u, u) \in E$ is possible.
N.B.

Named after Nicolaas de Bruijn, who introduced a related class of graphs in 1946, for a different problem.

Modelling our problem with de Bruijn graphs

Input: A collection $\mathcal{F}$ of strings.
First step: Generate all $k$-length substrings of fragments in $\mathcal{F}$.


Example
$\mathcal{F}=\{$ ATGGCGT, CAATGGC, CGTGCAA, GGCGTGC, TGCAATG $\}$.
For $k=3$, we get:
AAT, ATG, CAA, CGT, GCA, GCG, GGC, GTG, TGC, TGG.

Modelling our problem with de Bruijn graphs

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Modelling our problem with de Bruijn graphs

Now from the $k$-mers, we generate the $(k-1)$-length prefixes and suffixes: AA, AT, CA, CG, GC, GG, GT, TG. These are the vertices. The edges are the $k$-mers.

- $\mathcal{F}=\{$ ATGGCGT, CAATGGC, CGTGCAA, GGCGTGC, TGCAATG $\}, k=3$
- edges: AAT, ATG, CAA, CGT, GCA, GCG, GGC, GTG, TGC, TGG
- vertices: AA, AT, CA, CG, GC, GG, GT, TG

Modelling our problem with de Bruijn graphs

- edges: AAT, ATG, CAA, CGT, GCA, GCG, GGC, GTG, TGC, TGG (remember to only put an edge is the $k$-mer is present!)
- vertices: AA, AT, CA, CG, GC, GG, GT, TG

Modelling our problem with de Bruijn graphs

- edges: AAT, ATG, CAA, CGT, GCA, GCG, GGC, GTG, TGC, TGG (remember to only put an edge is the $k$-mer is present!)
- vertices: AA, AT, CA, CG, GC, GG, GT, TG


The numbers on the edges give an Eulerian cycle in this graph: ATGGCGTGCA

## Comparison to other models

Compare to modelling the same problem with overlap graphs: $\mathcal{F}=\{$ ATGGCGT, CAATGGC, CGTGCAA, GGCGTGC, TGCAATG $\}$


Genome: ATGGCGTGCAATGGCGT

Note that not all non-zero weight edges are included in the figure. The numbers on the edges give a Hamiltonian cycle: ATGGCGTGCA.

## Comparison to other models

Compare to modelling the same problem with overlap graphs using $k$-mers as nodes:

- $\mathcal{F}=\{$ ATGGCGT, CAATGGC, CGTGCAA, GGCGTGC, TGCAATG $\}, k=3$
- k-mers are nodes: AAT, ATG, CAA, CGT, GCA, GCG, GGC, GTG, TGC, TGG


Put an edge if the overlap equals $k-1$. The numbers on the edges give a Hamiltonian cycle: ATGGCGTGCA.

Practical strategies for applying de Bruijn graphs: all k-mers

Generating nearly all $k$-mers
In reality, only a small fraction of all 100 -mers (e.g.) are really sampled.
Solution: Take shorter $k$ than readlength. E.g. if reads have length approx.
100 , then taking $k=55$ will yield nearly all $k$-mers of the genome.
Ex.
In the example, not all 7 -mers are present as reads, but all 3-mers are:

- genome: ATGGCGTGCA
- 7-mers: ATGGCGT, CAATGGC, CGTGCAA, GGCGTGC, TGCAATG
- 3-mers: AAT, ATG, CAA, CGT, GCA, GCG, GGC, GTG, TGC, TGG

Practical strategies for applying de Bruijn graphs: errors

Errors is reads result in bubbles (= bulges) in the de Bruijn graph. This can be detected and handled, using multiplicity of $k$-mers (multigraphs!)


Practical strategies for applying de Bruijn graphs: errors Errors is reads result in bubbles (= bulges) in the de Bruijn graph. This can be detected and handled, via multiplicity of $k$-mers (multigraphs!) or of $(k-1)$-mers

E.g. the software Velvet (Zerbino and Birney, 2008) uses detection and elimination of bubbles and tips.

Practical strategies for applying de Bruijn graphs: repeats


Repeats can be detected using multiplicity of $k$-mers (edges). Again, using multigraphs (edges have multiplicities).

## Eulerian cycles in multigraphs

Theorem
A connected multigraph is Eulerian (has an Eulerian cycle) if and only if every vertex is balanced.

Now indegree $=$ sum of multiplicities of incoming edges (= number of incoming edges counted with their multiplicities), outdegree defined similarly.


Recall the Bridges of Königsberg problem.

- On page 8, is this the only Euler tour? If not, find the other circular string(s) which might give a solution. Do they also yield a superstring for the input fragments of length 7 ?
- Repeat the algorithm from p. 7-8 with $k=4$. How many Euler tours exist now?

Homework

Origins of de Bruijn graphs



[^0]:    ${ }^{1}$ These slides mainly based on Compeau, Pevzner, Tesler: How to apply de Bruijn graphs to genome assembly, Nature Biotechnology 29 (11).

