

Example-Guided Abstraction Simplification

Francesco Ranzato
University of Padova

Abstraction Refinements

- ❖ Widely used paradigm in static analysis and verification, e.g. CEGAR

Abstraction Refinements

- ❖ Widely used paradigm in static analysis and verification, e.g. CEGAR
- ❖ Basic principles

Abstraction Refinements

- ❖ Widely used paradigm in static analysis and verification, e.g. CEGAR
- ❖ Basic principles
 - ◆ Identify when and how to refine the underlying abstraction, e.g. abstract domain

Abstraction Refinements

- ❖ Widely used paradigm in static analysis and verification, e.g. CEGAR
- ❖ Basic principles
 - ◆ Identify when and how to refine the underlying abstraction, e.g. abstract domain
 - ◆ Goal: remove some false alarms or spurious traces

Abstraction Simplifications

- ❖ Few examples in static analysis and verification

Abstraction Simplifications

- ❖ Few examples in static analysis and verification
- ❖ Basic principles

Abstraction Simplifications

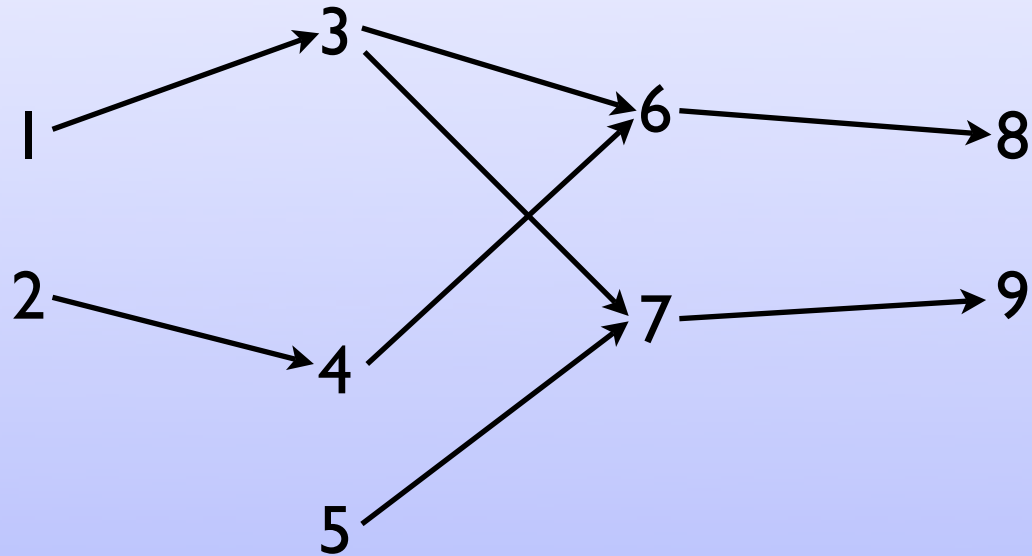
- ❖ Few examples in static analysis and verification
- ❖ Basic principles
 - ◆ Identify when and how to simplify the underlying abstraction

Abstraction Simplifications

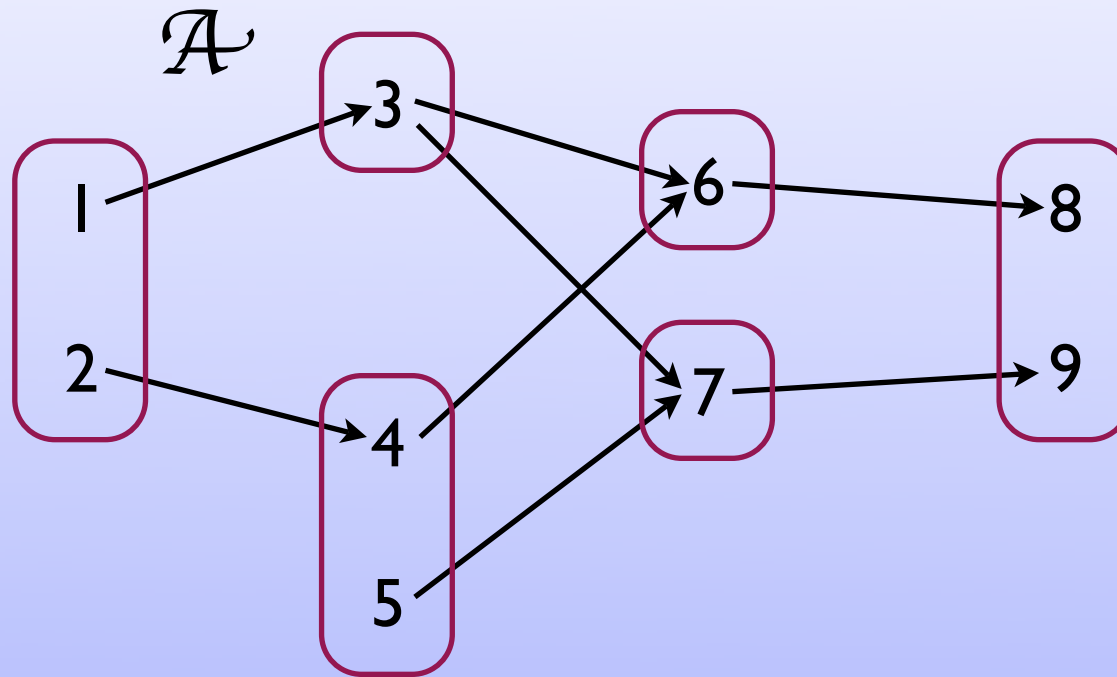
- ❖ Few examples in static analysis and verification
- ❖ Basic principles
 - ◆ Identify when and how to simplify the underlying abstraction
 - ◆ Goal: maintain the same approximate behaviour

Example in abstract model checking

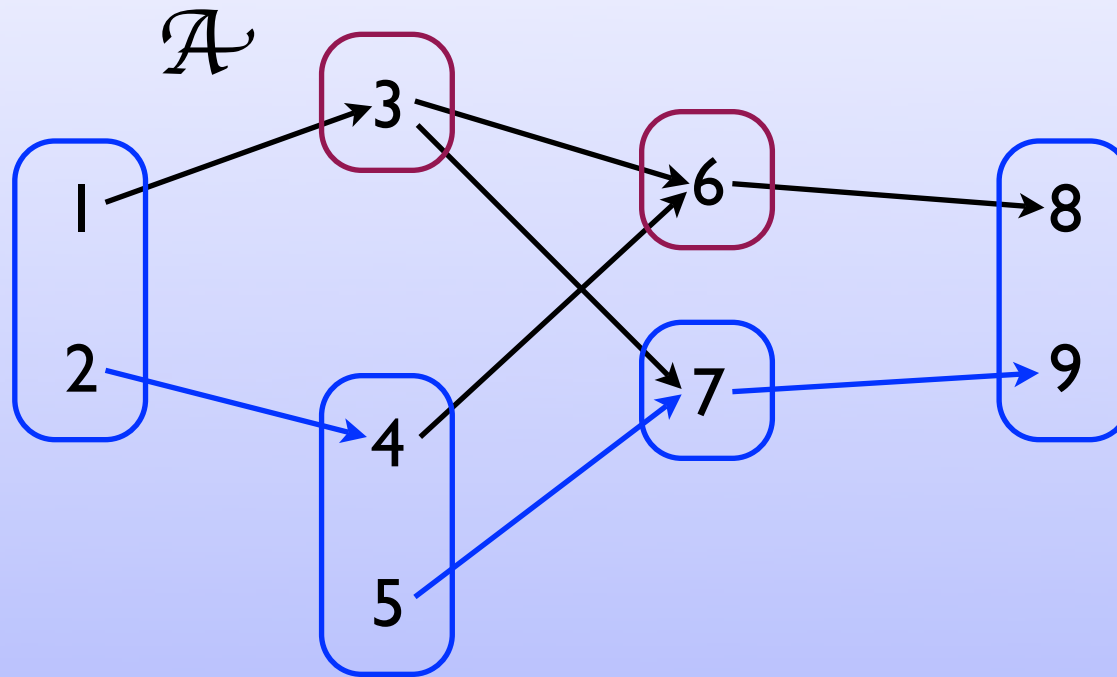
Example in abstract model checking



Example in abstract model checking

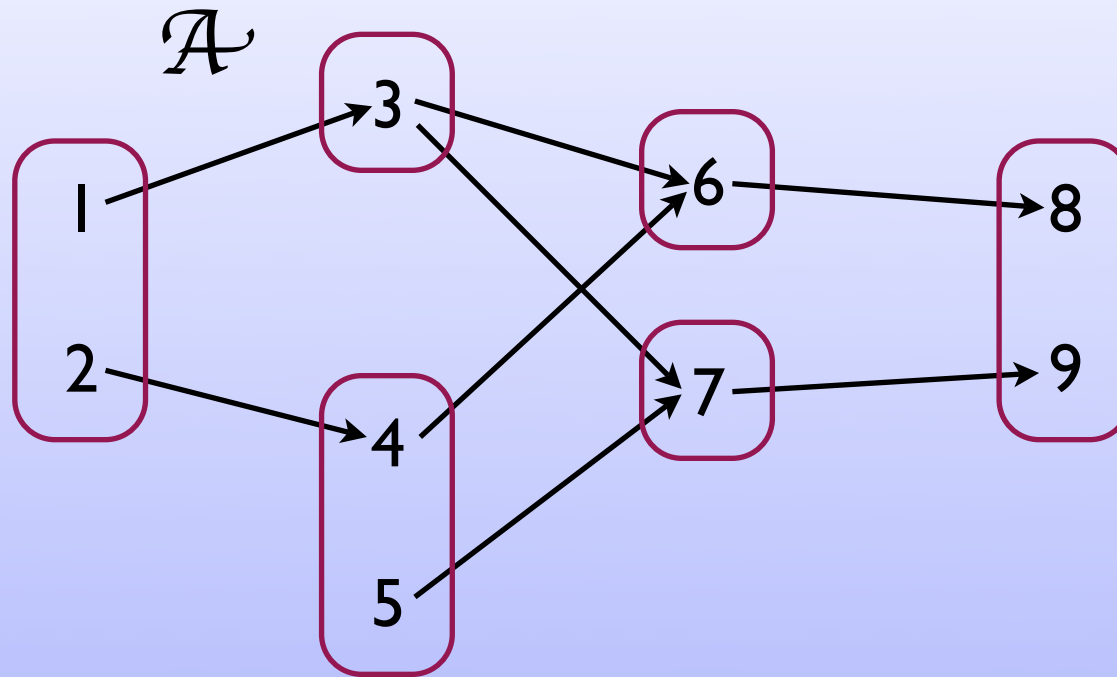


Example in abstract model checking

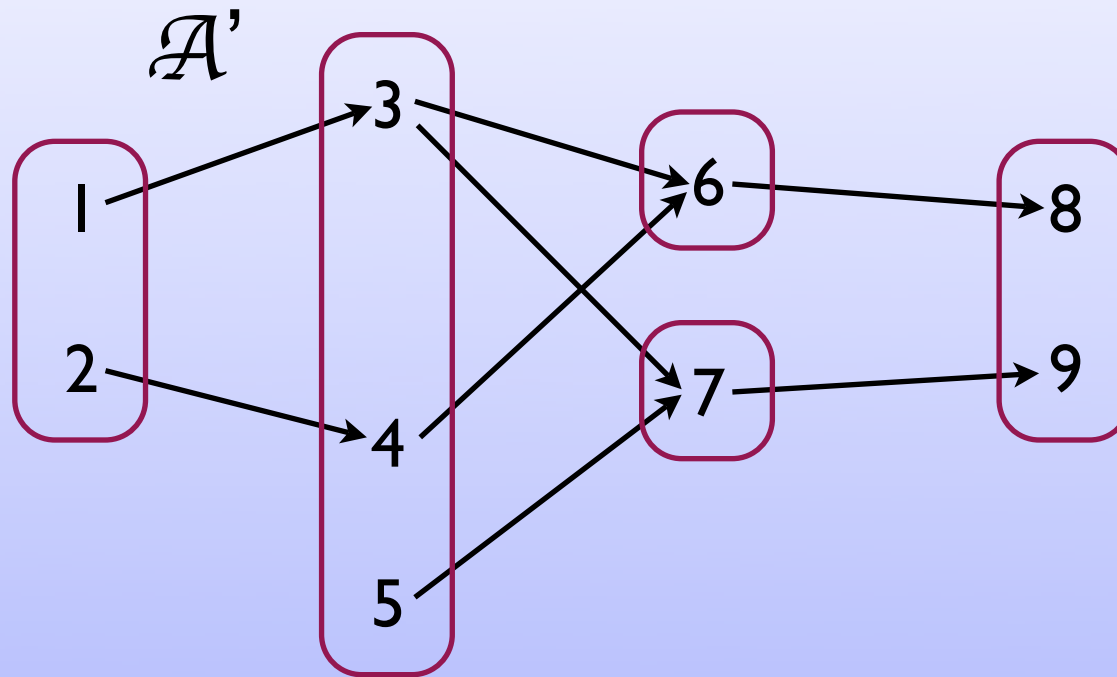


Spurious abstract path: $[1,2] \rightarrow [4,5] \rightarrow [7] \rightarrow [8,9]$

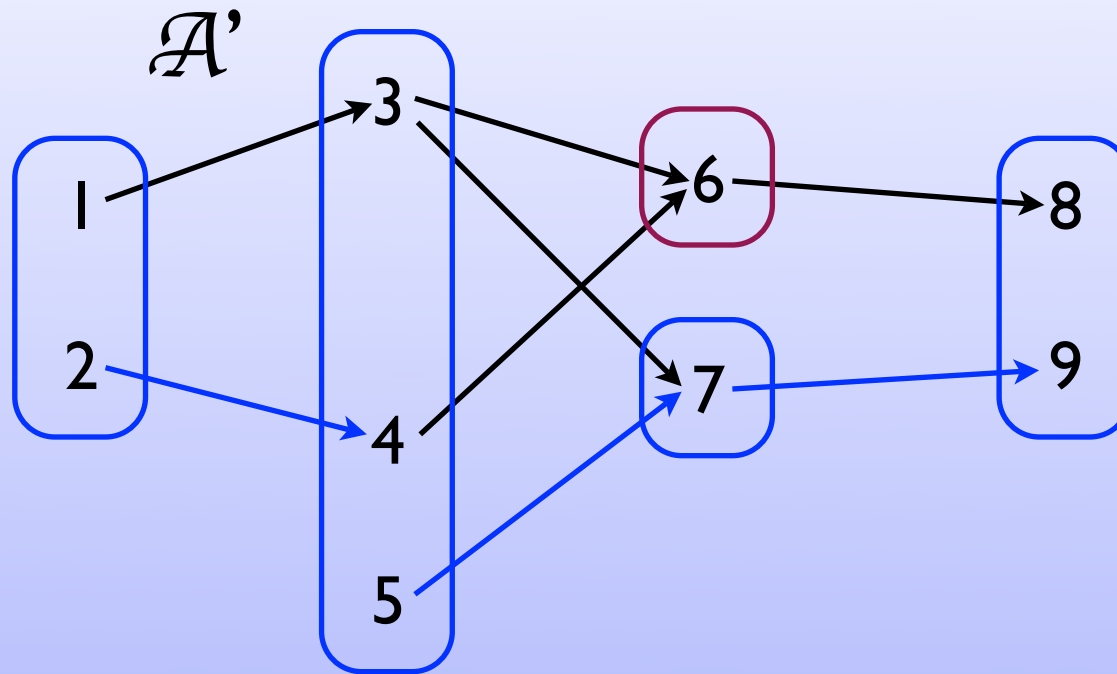
Example in abstract model checking



Example in abstract model checking

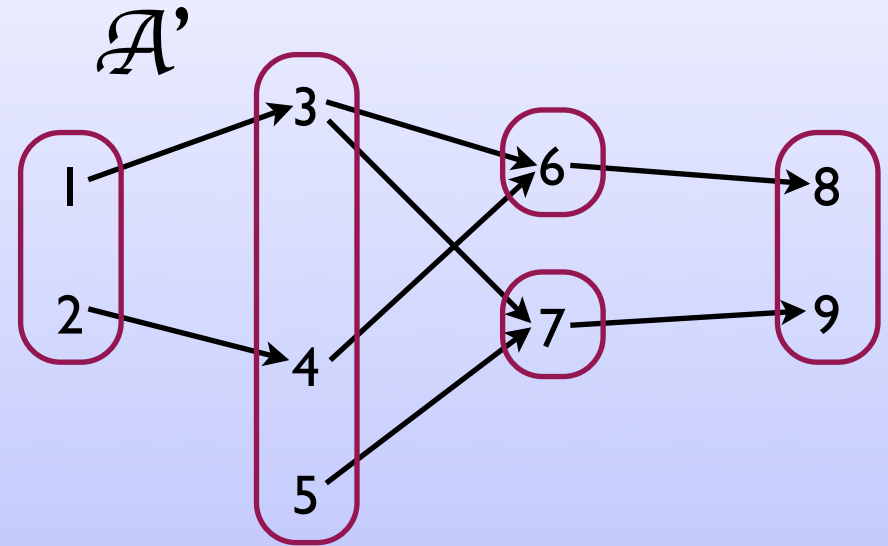
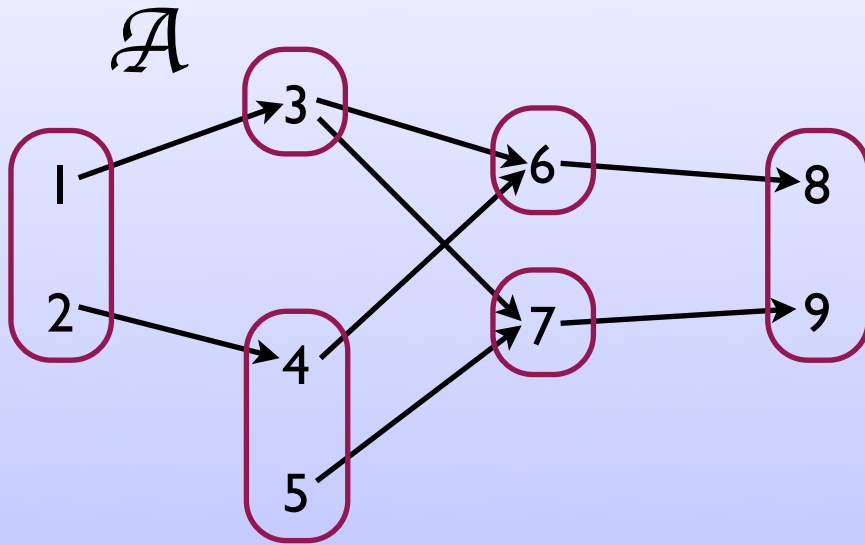


Example in abstract model checking

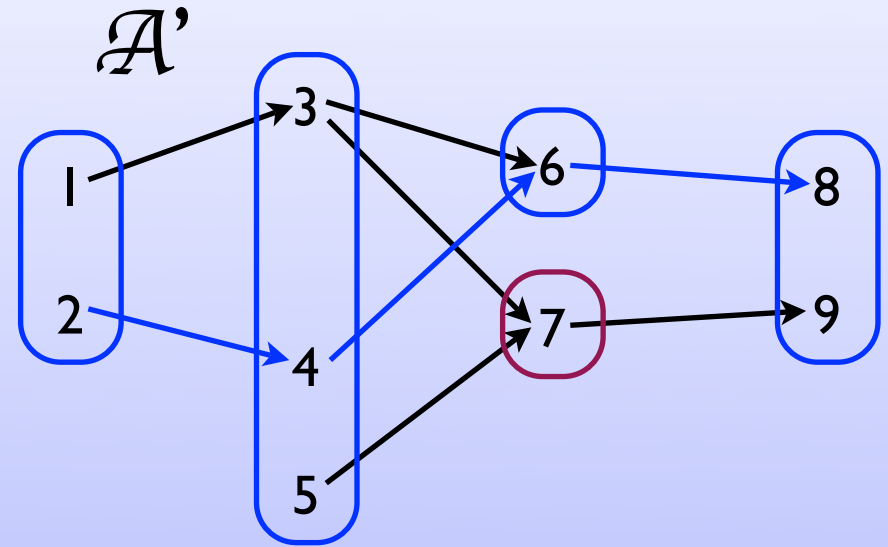
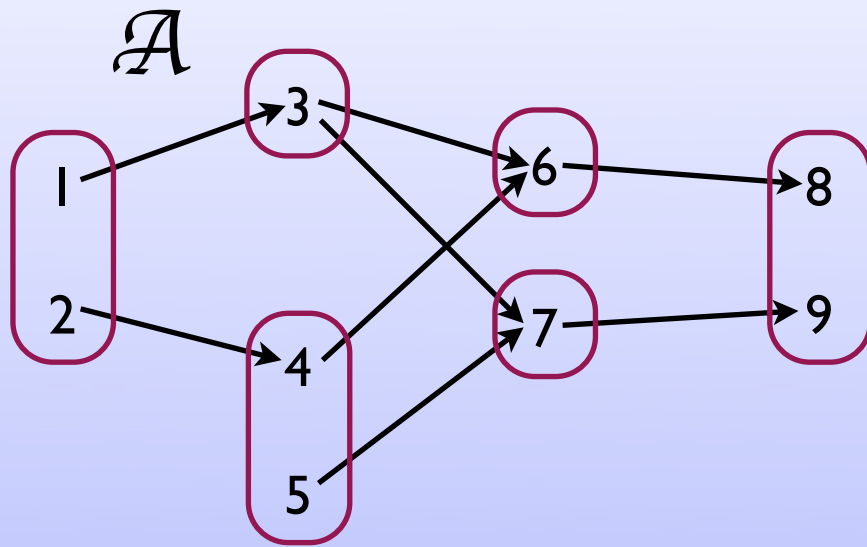


Spurious abstract path: $[1,2] \rightarrow [3,4,5] \rightarrow [7] \rightarrow [8,9]$

Example in abstract model checking

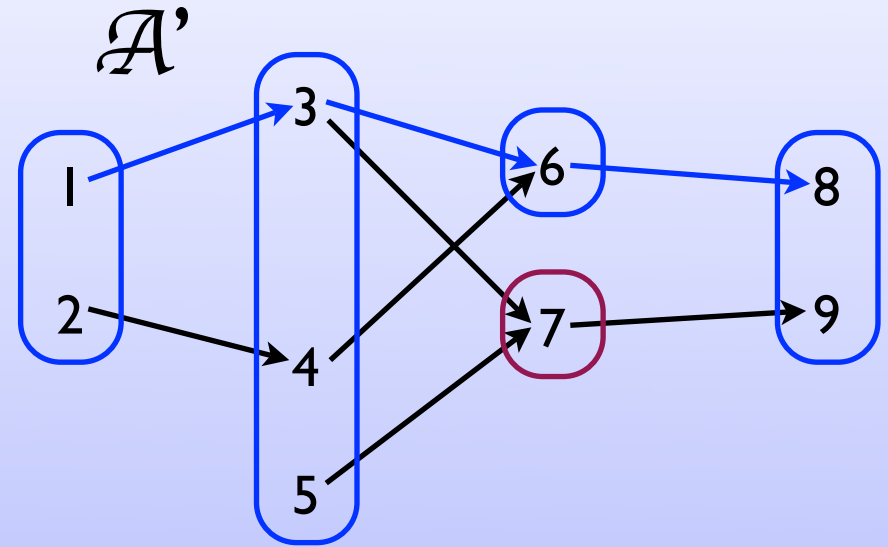
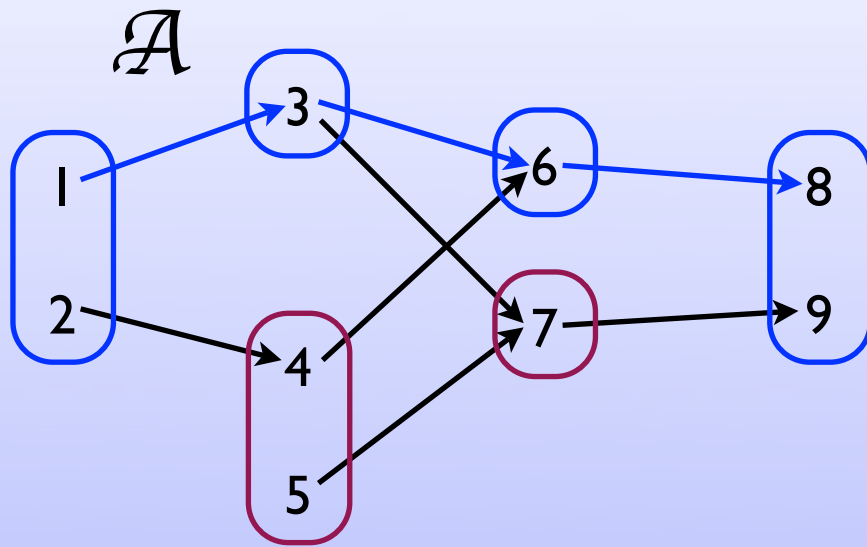


Example in abstract model checking



Not spurious abstract path in \mathcal{A}' : $[1,2] \rightarrow [3,4,5] \rightarrow [6] \rightarrow [8,9]$

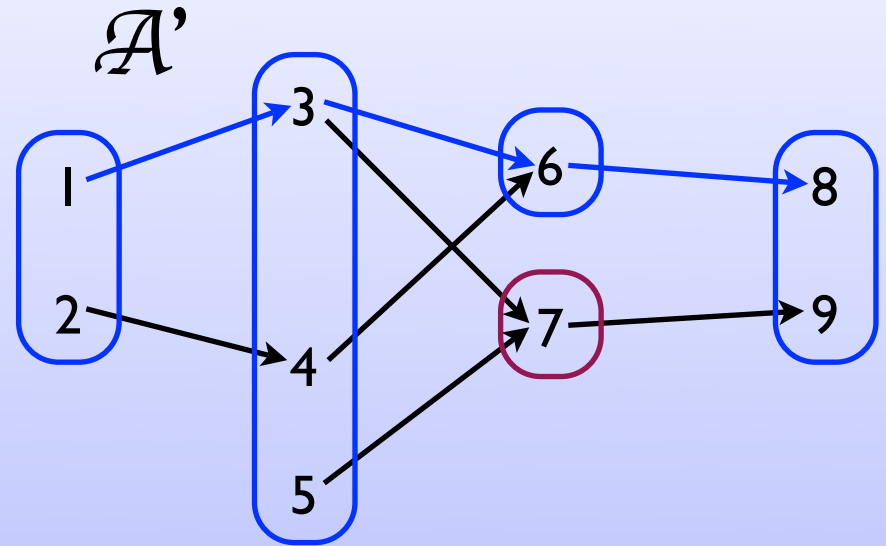
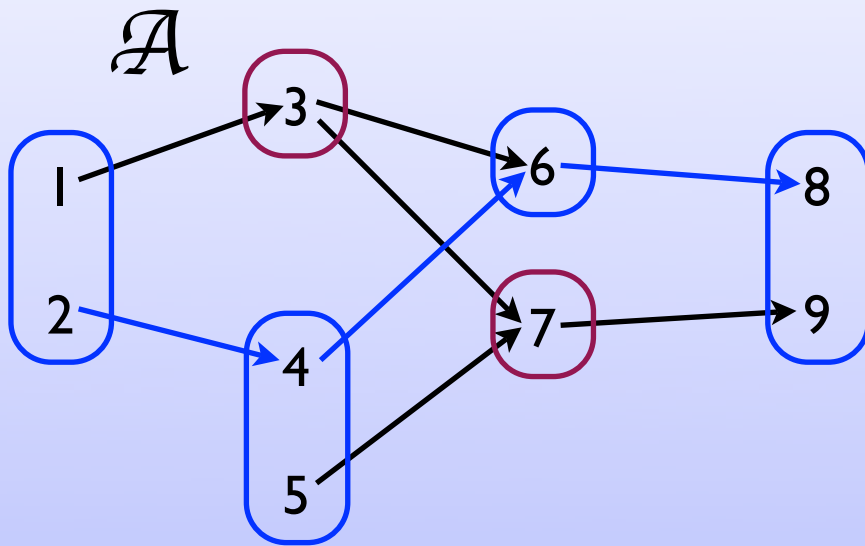
Example in abstract model checking



Not spurious abstract path in \mathcal{A}' : $[1,2] \rightarrow [3,4,5] \rightarrow [6] \rightarrow [8,9]$

Not spurious abstract path in \mathcal{A} : $[1,2] \rightarrow [3] \rightarrow [6] \rightarrow [8,9]$

Example in abstract model checking

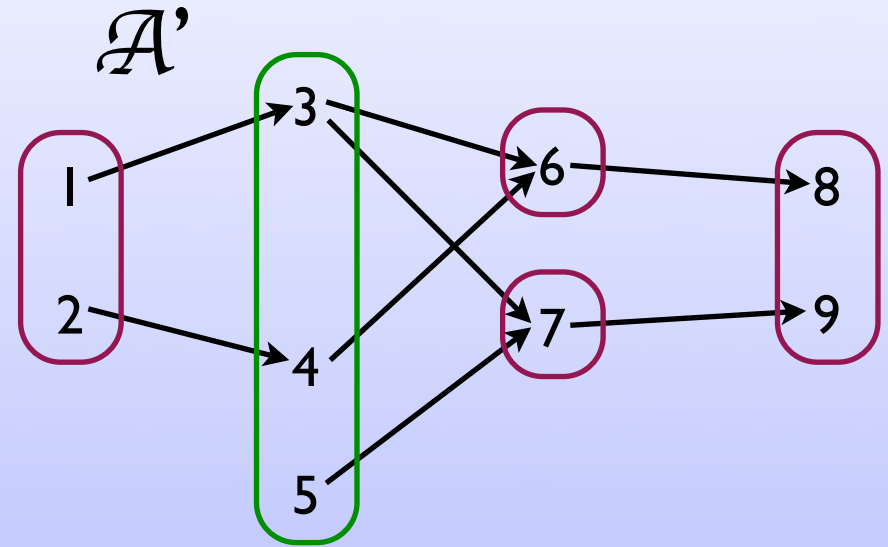
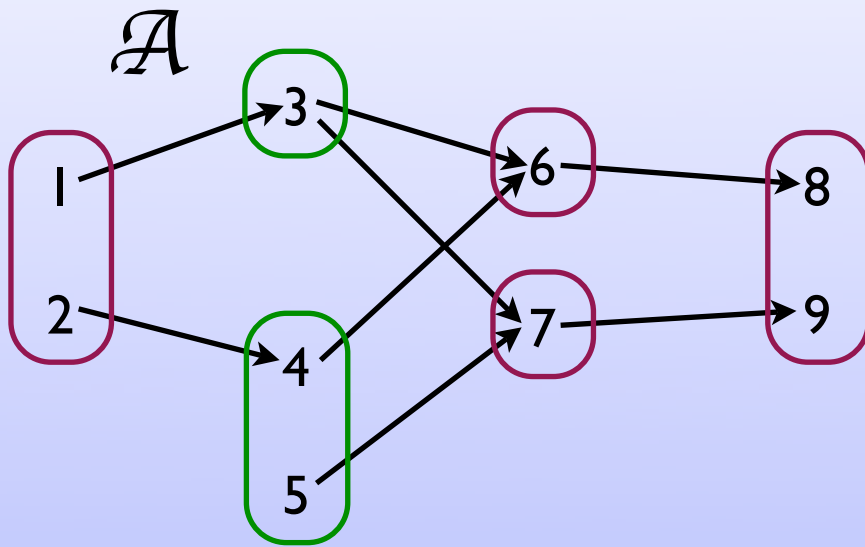


Not spurious abstract path in \mathcal{A}' : $[1,2] \rightarrow [3,4,5] \rightarrow [6] \rightarrow [8,9]$

Not spurious abstract path in \mathcal{A} : $[1,2] \rightarrow [3] \rightarrow [6] \rightarrow [8,9]$

Not spurious abstract path in \mathcal{A} : $[1,2] \rightarrow [4,5] \rightarrow [6] \rightarrow [8,9]$

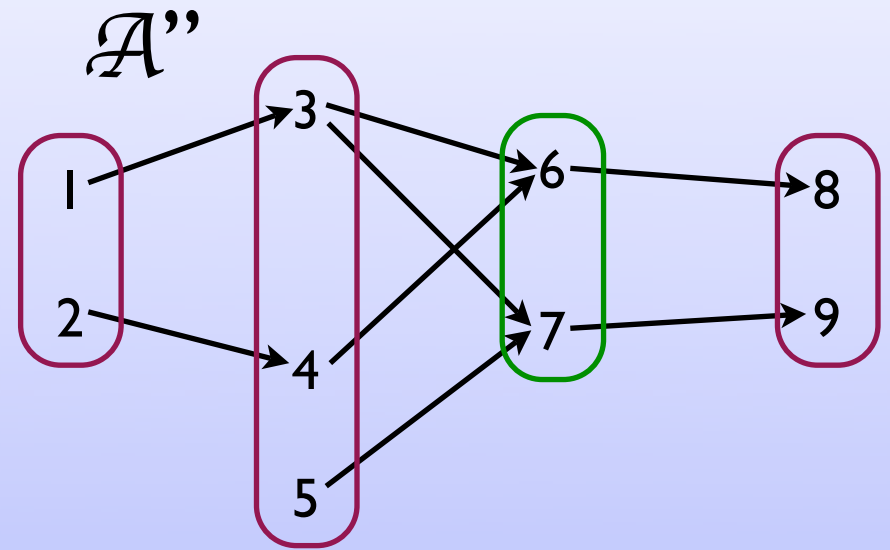
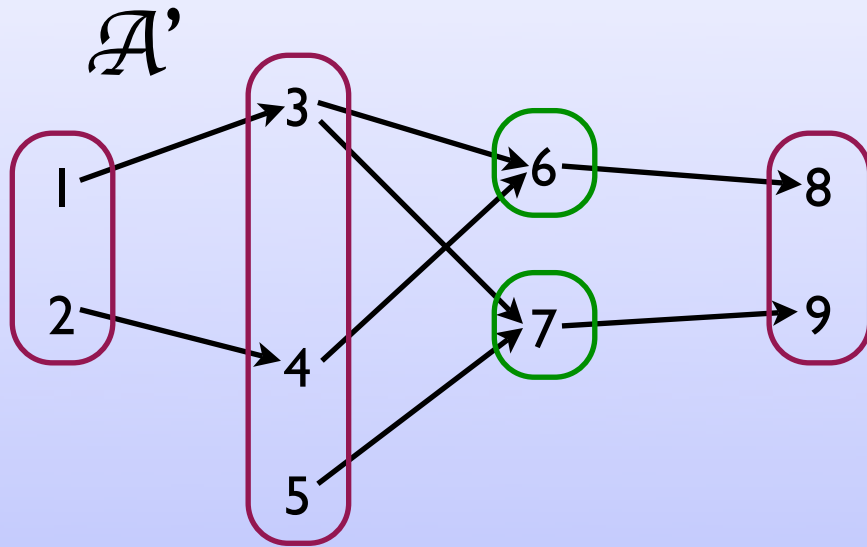
Example in abstract model checking



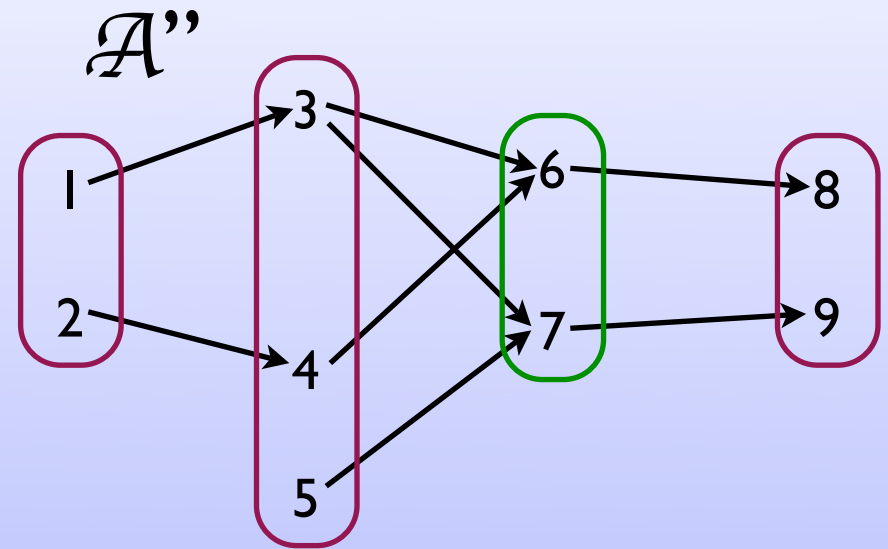
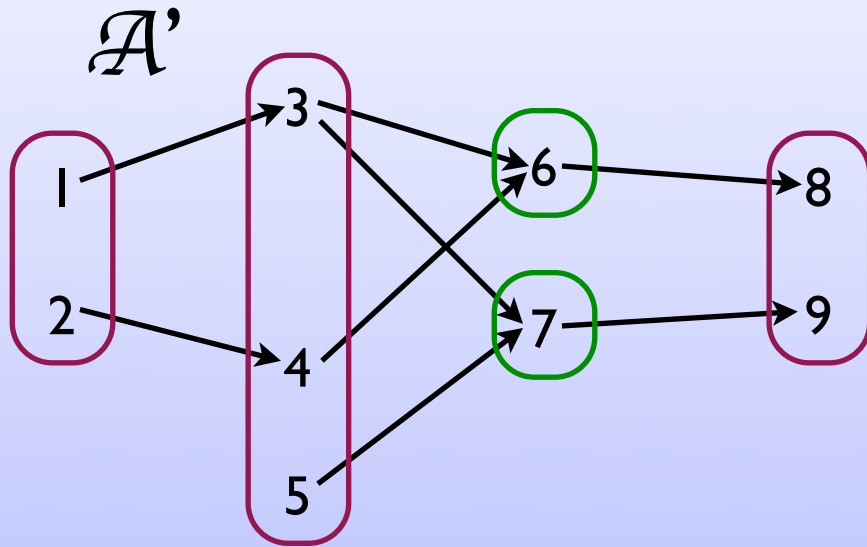
\mathcal{A}' keeps the same examples of \mathcal{A} :

if π' is spurious in \mathcal{A}' then there exists a spurious π in \mathcal{A} such that $\alpha(\pi) = \pi'$

Example in abstract model checking

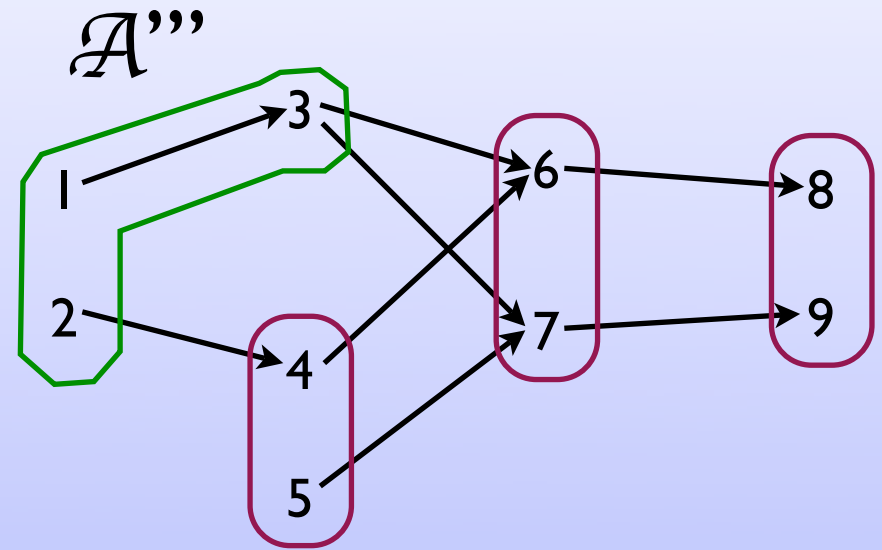
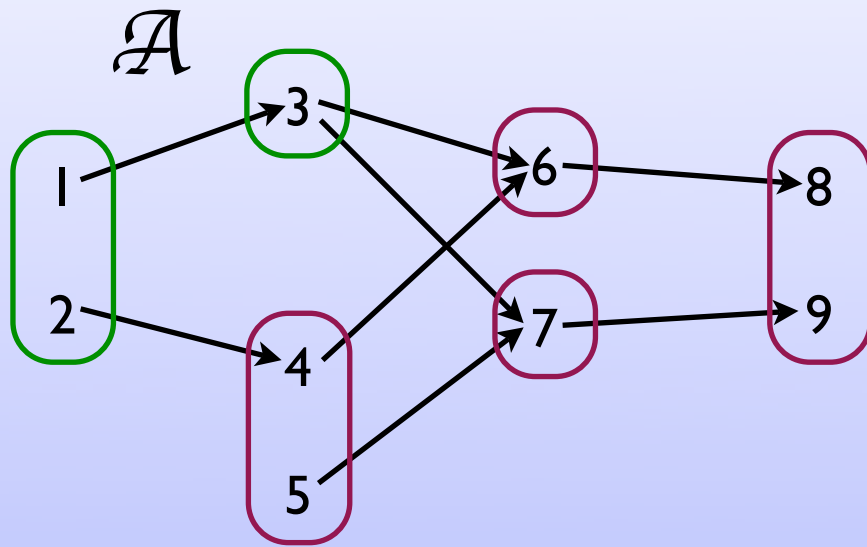


Example in abstract model checking

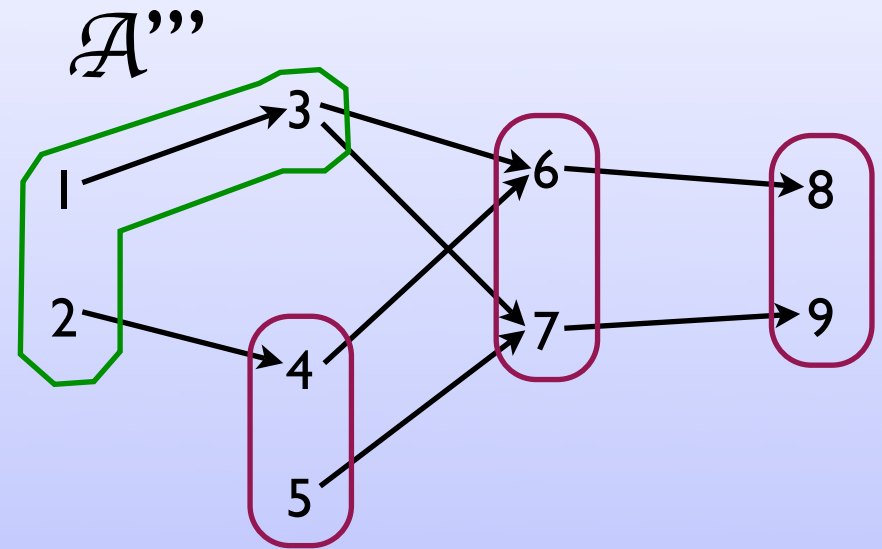
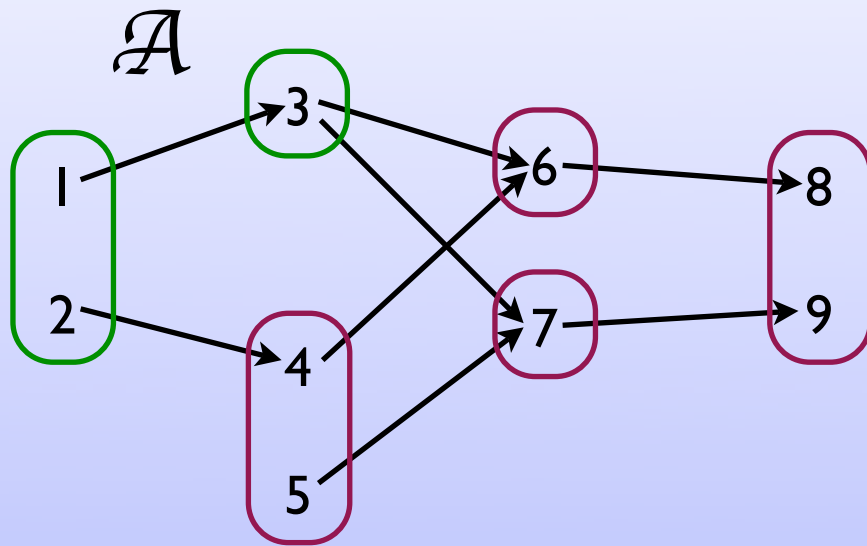


\mathcal{A}'' keeps the same examples of \mathcal{A}'

Example in abstract model checking

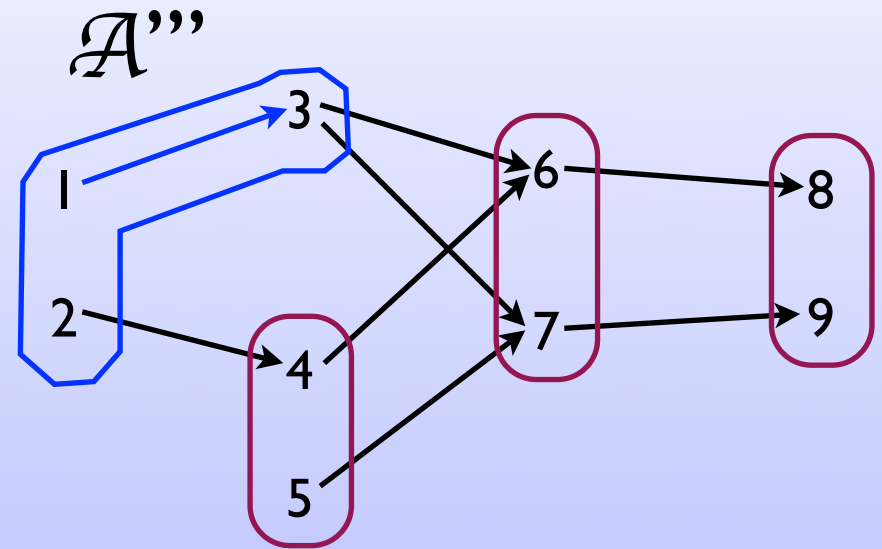
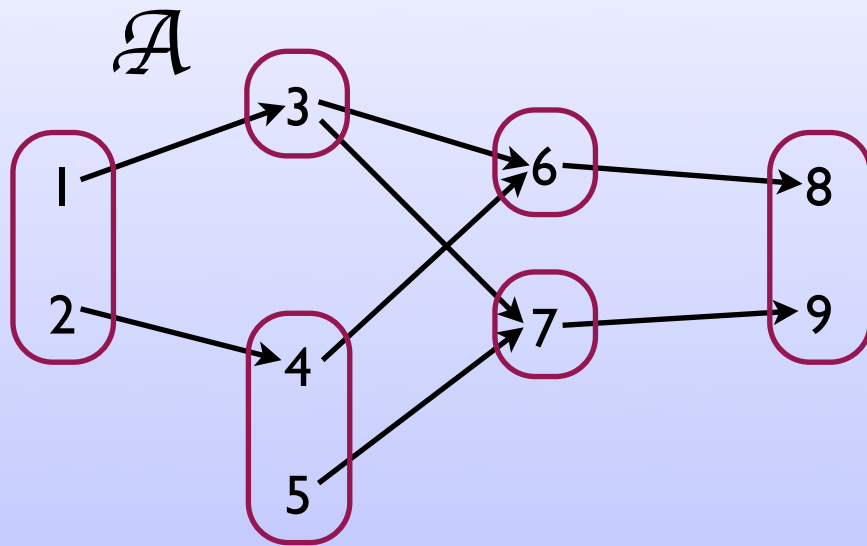


Example in abstract model checking



\mathcal{A}''' doesn't keep the same examples of \mathcal{A}

Example in abstract model checking



\mathcal{A}''' doesn't keep the same examples of \mathcal{A}

Spurious loop path in \mathcal{A}''' : $[1,2,3] \rightarrow [1,2,3] \rightarrow [1,2,3] \rightarrow \dots$

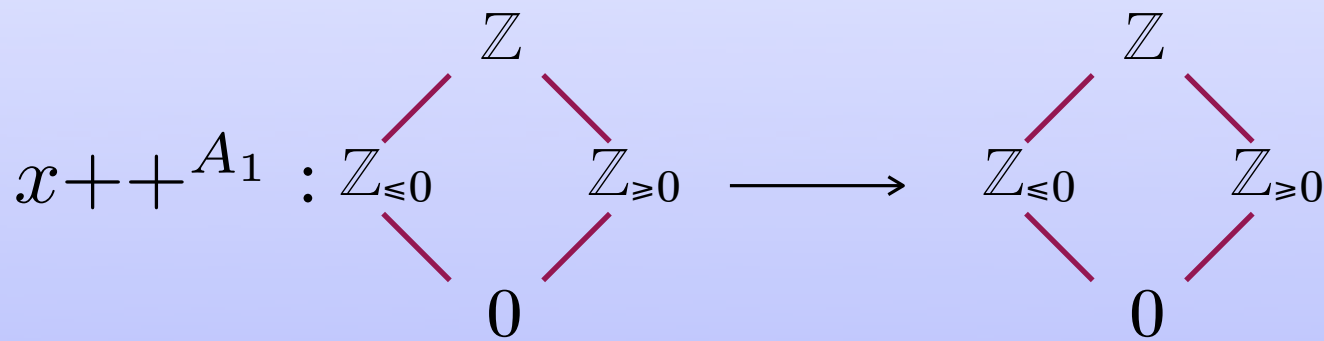
BUT no corresponding spurious path in \mathcal{A}

Example in abstract interpretation

$$x++ : \wp(\mathbb{Z}) \rightarrow \wp(\mathbb{Z})$$

Example in abstract interpretation

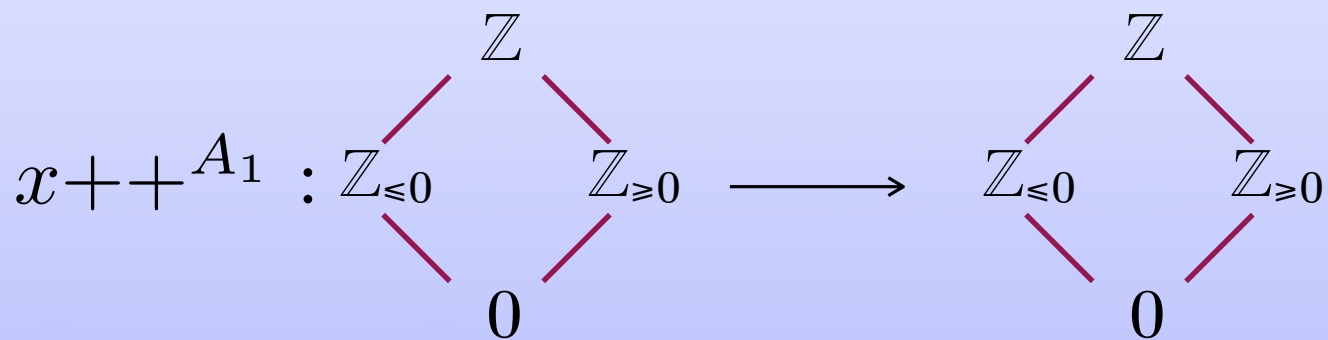
$$x++ : \wp(\mathbb{Z}) \rightarrow \wp(\mathbb{Z})$$



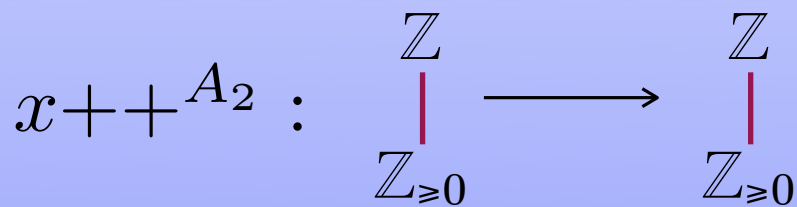
$0++ = \mathbb{Z}_{\geq 0}$
$\mathbb{Z}_{\leq 0}++ = \mathbb{Z}$
$\mathbb{Z}_{\geq 0}++ = \mathbb{Z}_{\geq 0}$
$\mathbb{Z}++ = \mathbb{Z}$

Example in abstract interpretation

$$x++ : \wp(\mathbb{Z}) \rightarrow \wp(\mathbb{Z})$$

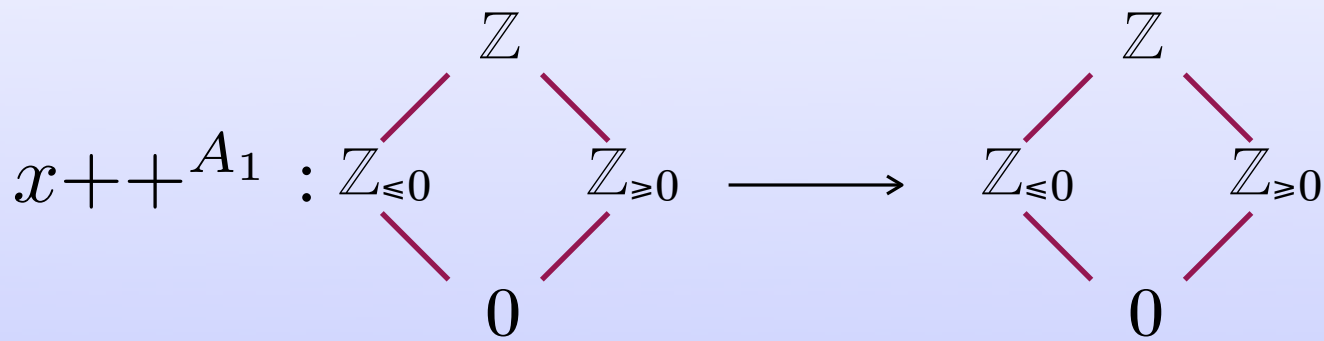


$$\begin{aligned} 0++ &= \mathbb{Z}_{\geq 0} \\ \mathbb{Z}_{\leq 0}++ &= \mathbb{Z} \\ \mathbb{Z}_{\geq 0}++ &= \mathbb{Z}_{\geq 0} \\ \mathbb{Z}++ &= \mathbb{Z} \end{aligned}$$



$$\begin{aligned} \mathbb{Z}_{\geq 0}++ &= \mathbb{Z}_{\geq 0} \\ \mathbb{Z}++ &= \mathbb{Z} \end{aligned}$$

Example in abstract interpretation

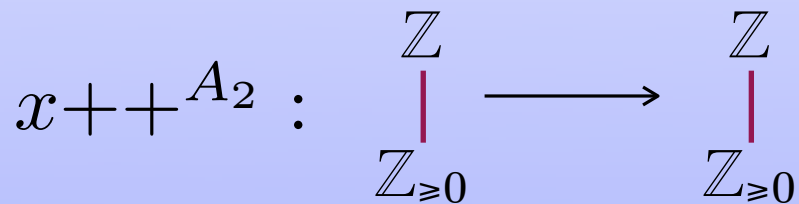


$$0_{++} = \mathbb{Z}_{\geq 0}$$

$$\mathbb{Z}_{\leq 0}_{++} = \mathbb{Z}$$

$$\mathbb{Z}_{\geq 0}_{++} = \mathbb{Z}_{\geq 0}$$

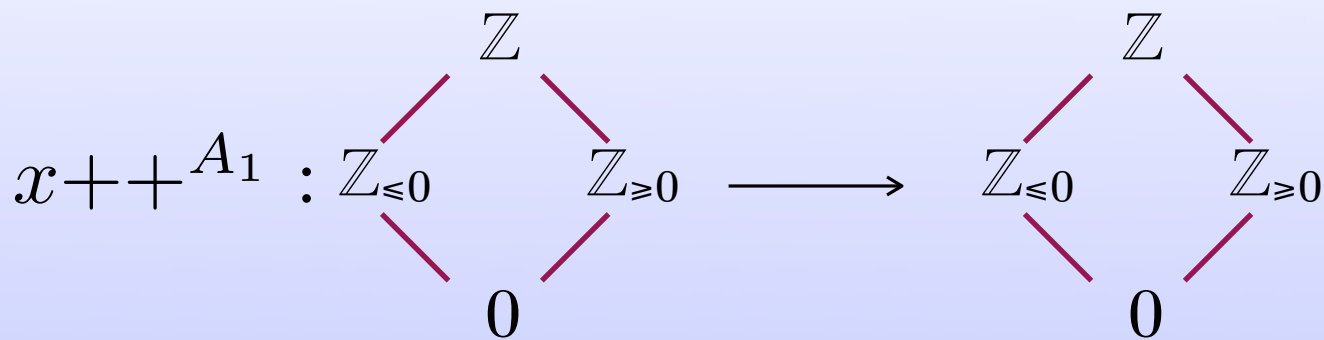
$$\mathbb{Z}_{++} = \mathbb{Z}$$



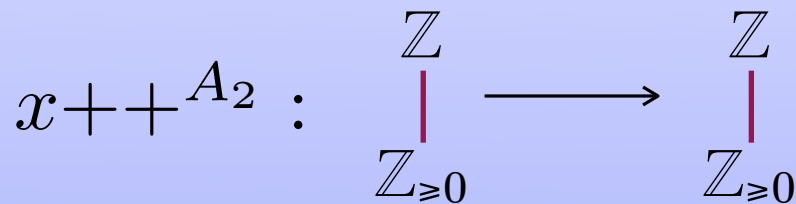
$$\mathbb{Z}_{\geq 0}_{++} = \mathbb{Z}_{\geq 0}$$

$$\mathbb{Z}_{++} = \mathbb{Z}$$

Example in abstract interpretation



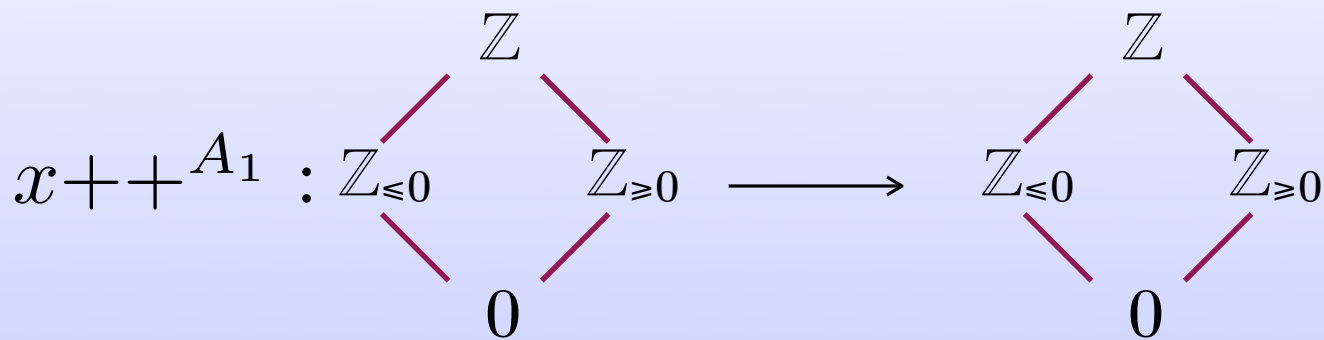
$$\begin{aligned} 0_{++} &= \mathbb{Z}_{\geq 0} \\ \mathbb{Z}_{\leq 0}_{++} &= \mathbb{Z} \\ \mathbb{Z}_{\geq 0}_{++} &= \mathbb{Z}_{\geq 0} \\ \mathbb{Z}_{++} &= \mathbb{Z} \end{aligned}$$



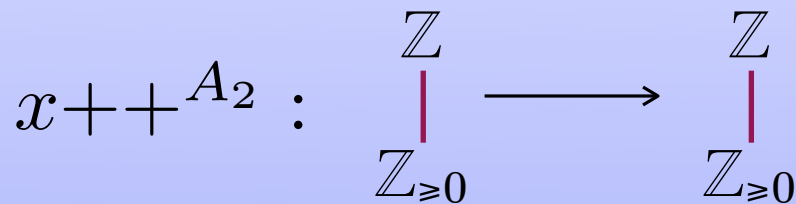
$$\begin{aligned} \mathbb{Z}_{\geq 0}_{++} &= \mathbb{Z}_{\geq 0} \\ \mathbb{Z}_{++} &= \mathbb{Z} \end{aligned}$$

$x_{++}^{A_1}, x_{++}^{A_2}$ encode the same function in $\wp(\mathbb{Z}) \rightarrow \wp(\mathbb{Z})$

Example in abstract interpretation



$$\begin{aligned} 0_{++} &= \mathbb{Z}_{\geq 0} \\ \mathbb{Z}_{\leq 0}_{++} &= \mathbb{Z} \\ \mathbb{Z}_{\geq 0}_{++} &= \mathbb{Z}_{\geq 0} \\ \mathbb{Z}_{++} &= \mathbb{Z} \end{aligned}$$

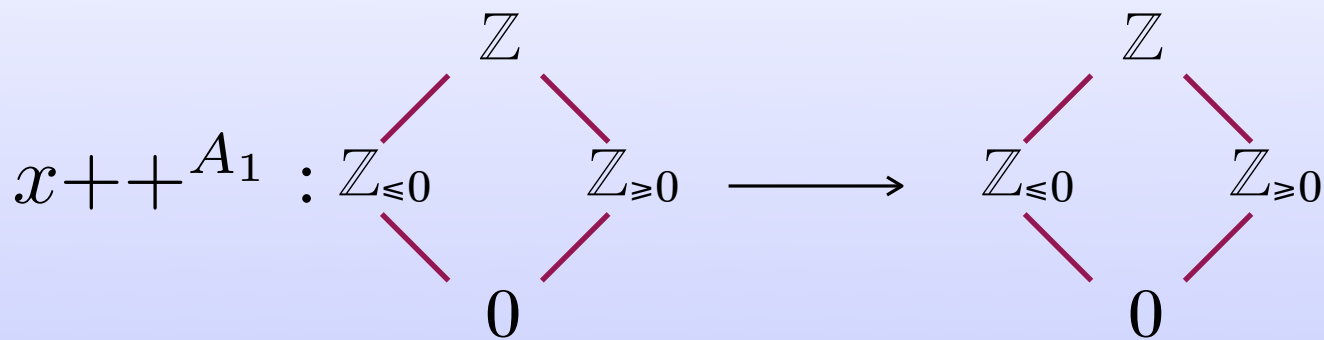


$$\begin{aligned} \mathbb{Z}_{\geq 0}_{++} &= \mathbb{Z}_{\geq 0} \\ \mathbb{Z}_{++} &= \mathbb{Z} \end{aligned}$$

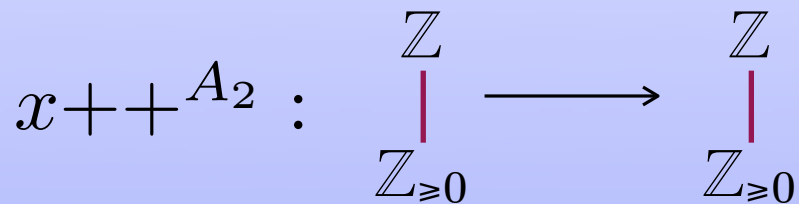
$x_{++}^{A_1}, x_{++}^{A_2}$ encode the same function in $\wp(\mathbb{Z}) \rightarrow \wp(\mathbb{Z})$

$$(\gamma_{A_1} \circ \alpha_{A_1}) \circ x_{++} \circ (\gamma_{A_1} \circ \alpha_{A_1}) = (\gamma_{A_2} \circ \alpha_{A_2}) \circ x_{++} \circ (\gamma_{A_2} \circ \alpha_{A_2})$$

Example in abstract interpretation



$$\begin{aligned} 0_{++} &= \mathbb{Z}_{\geq 0} \\ \mathbb{Z}_{\leq 0}_{++} &= \mathbb{Z} \\ \mathbb{Z}_{\geq 0}_{++} &= \mathbb{Z}_{\geq 0} \\ \mathbb{Z}_{++} &= \mathbb{Z} \end{aligned}$$

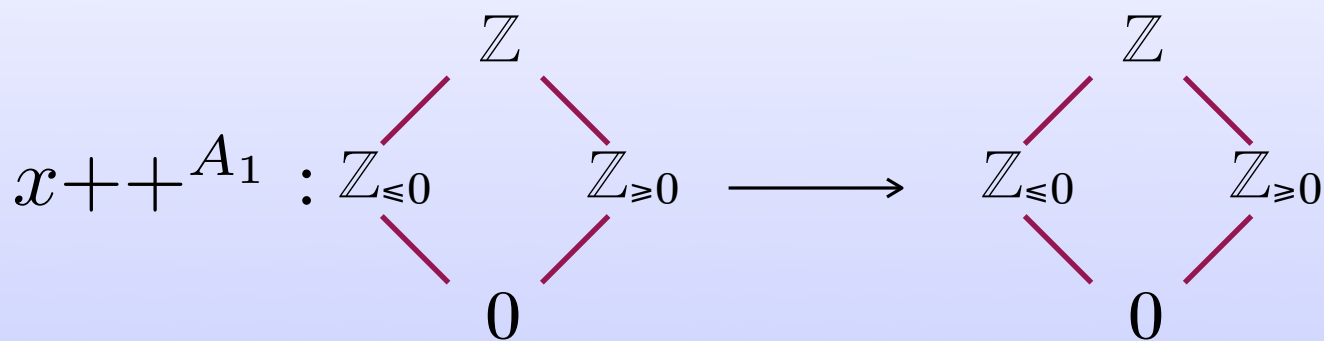


$$\begin{aligned} \mathbb{Z}_{\geq 0}_{++} &= \mathbb{Z}_{\geq 0} \\ \mathbb{Z}_{++} &= \mathbb{Z} \end{aligned}$$

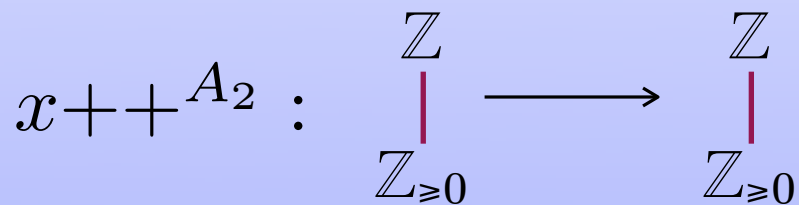
$x_{++}^{A_1}, x_{++}^{A_2}$ encode the same function in $\wp(\mathbb{Z}) \rightarrow \wp(\mathbb{Z})$

0 and $\mathbb{Z}_{\leq 0}$ are “irrelevant” in A_1 for approximating x_{++}

Example in abstract interpretation



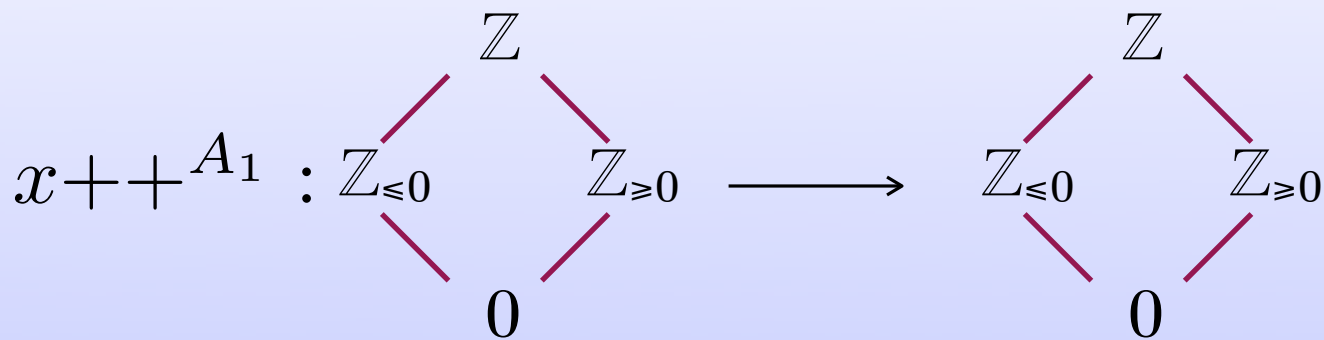
$$\begin{aligned} 0_{++} &= \mathbb{Z}_{\geq 0} \\ \mathbb{Z}_{\leq 0}_{++} &= \mathbb{Z} \\ \mathbb{Z}_{\geq 0}_{++} &= \mathbb{Z}_{\geq 0} \\ \mathbb{Z}_{++} &= \mathbb{Z} \end{aligned}$$



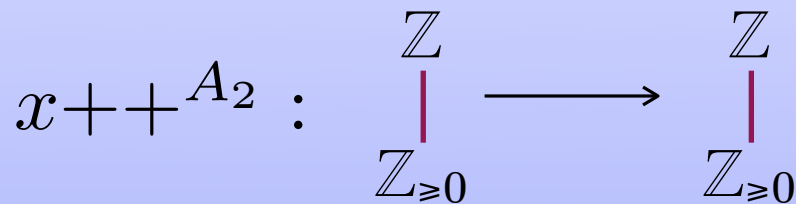
$$\begin{aligned} \mathbb{Z}_{\geq 0}_{++} &= \mathbb{Z}_{\geq 0} \\ \mathbb{Z}_{++} &= \mathbb{Z} \end{aligned}$$

0 and $\mathbb{Z}_{\leq 0}$ are “irrelevant” in A_1 for approximating x_{++}

Example in abstract interpretation



$$\begin{aligned} 0^{++} &= \mathbb{Z}_{\geq 0} \\ \mathbb{Z}_{\leq 0}^{++} &= \mathbb{Z} \\ \mathbb{Z}_{\geq 0}^{++} &= \mathbb{Z}_{\geq 0} \\ \mathbb{Z}^{++} &= \mathbb{Z} \end{aligned}$$



$$\begin{aligned} \mathbb{Z}_{\geq 0}^{++} &= \mathbb{Z}_{\geq 0} \\ \mathbb{Z}^{++} &= \mathbb{Z} \end{aligned}$$

0 and $\mathbb{Z}_{\leq 0}$ are “irrelevant” in A_1 for approximating x^{++}

$$\{0, -2, -7\} \xrightarrow{A_1} \mathbb{Z}_{\leq 0} \xrightarrow{++} \{\mathbf{x} \leq 1\} \xrightarrow{A_1} \mathbb{Z}$$

$$\{0, -2, -7\} \xrightarrow{A_2} \mathbb{Z} \xrightarrow{++} \mathbb{Z} \xrightarrow{A_2} \mathbb{Z}$$

Abstract interpretation

- ❖ Problem formalized in **abstract interpretation**

Abstract interpretation

- ❖ Problem formalized in **abstract interpretation**
- ❖ Main ingredients

Abstract interpretation

- ❖ Problem formalized in **abstract interpretation**
- ❖ Main ingredients
 - ◆ Approximation formalized by **partial orders**

Abstract interpretation

- ❖ Problem formalized in **abstract interpretation**
- ❖ Main ingredients
 - ◆ Approximation formalized by **partial orders**
 - ◆ **Concrete domain C_{\leq}**

Abstract interpretation

- ❖ Problem formalized in **abstract interpretation**
- ❖ Main ingredients
 - ◆ Approximation formalized by **partial orders**
 - ◆ **Concrete domain** C_{\leq}
 - ◆ Abstractions A_{\leq} formalized by **Galois connections** α/γ

Abstract interpretation

- ❖ Problem formalized in **abstract interpretation**
- ❖ Main ingredients
 - ◆ Approximation formalized by **partial orders**
 - ◆ **Concrete domain** C_{\leq}
 - ◆ Abstractions A_{\leq} formalized by **Galois connections** α/γ
 - ◆ Concrete objects c have **best correct approximations** $\alpha(c)$

Abstract interpretation

- ❖ Problem formalized in **abstract interpretation**
- ❖ Main ingredients
 - ◆ Approximation formalized by **partial orders**
 - ◆ **Concrete domain** C_{\leq}
 - ◆ Abstractions A_{\leq} formalized by **Galois connections** α/γ
 - ◆ Concrete objects c have **best correct approximations** $\alpha(c)$
 - ◆ Semantic functions $f : C \rightarrow C$ have **best correct approximations** $f^A \stackrel{\text{def}}{=} \alpha \circ f \circ \gamma : A \rightarrow A$

Correctness Kernel

Concrete semantic function $f: C \rightarrow C$

Abstract domain $A \in \text{Abs}(C)$

$\alpha_A: C \rightarrow A$ $\gamma_A: A \rightarrow C$

Abstract domain $B \in \text{Abs}(C)$

$\alpha_B: C \rightarrow B$ $\gamma_B: B \rightarrow C$

Correctness Kernel

Concrete semantic function $f: C \rightarrow C$

Abstract domain $A \in \text{Abs}(C)$

$\alpha_A: C \rightarrow A$ $\gamma_A: A \rightarrow C$

Abstract domain $B \in \text{Abs}(C)$

$\alpha_B: C \rightarrow B$ $\gamma_B: B \rightarrow C$

$$f^A = f^B \text{ when} \\ (\gamma_A \alpha_A) \circ f \circ (\gamma_A \alpha_A) = (\gamma_B \alpha_B) \circ f \circ (\gamma_B \alpha_B)$$

That is, the best correct approximations of function f in A and B coincide when encoded within C

Correctness Kernel

$$f^A = f^B \text{ when}$$
$$(\gamma_A \alpha_A) \circ f \circ (\gamma_A \alpha_A) = (\gamma_B \alpha_B) \circ f \circ (\gamma_B \alpha_B)$$

Correctness Kernel

$$f^A = f^B \text{ when} \\ (\gamma_A \alpha_A) \circ f \circ (\gamma_A \alpha_A) = (\gamma_B \alpha_B) \circ f \circ (\gamma_B \alpha_B)$$

Correctness kernel $K_f(A)$ of A for f:

$K_f(A) \stackrel{\text{def}}{=} \text{most abstract domain } B \text{ such that } f^B = f^A$

Correctness Kernel

$$f^A = f^B \text{ when} \\ (\gamma_A \alpha_A) \circ f \circ (\gamma_A \alpha_A) = (\gamma_B \alpha_B) \circ f \circ (\gamma_B \alpha_B)$$

Main Technical Result

If $f \circ (\gamma_A \alpha_A)$ is continuous then $K_f(A)$ exists and

$$K_f(A) = \text{img}(f^A) \cup \bigcup_{y \in \text{img}(f^A)} \max(\{x \in A \mid f^A(x) = y\})$$

Correctness Kernel

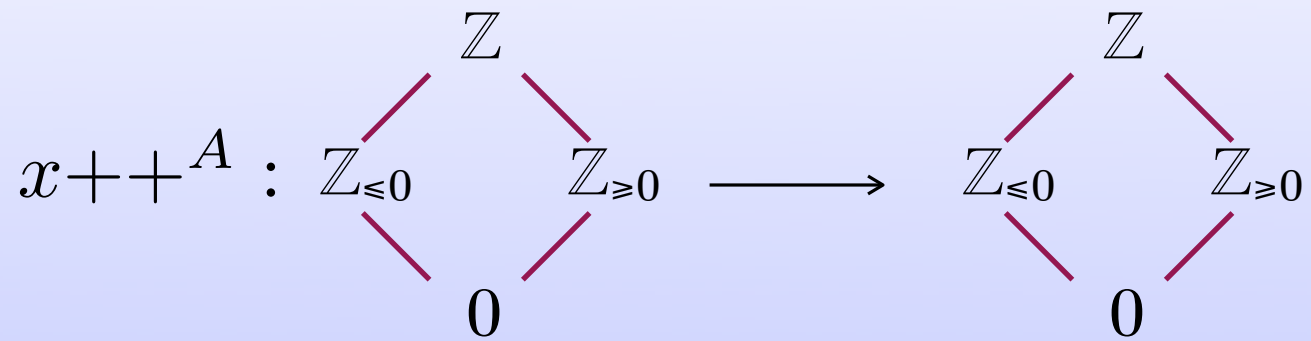
$$f^A = f^B \text{ when} \\ (\gamma_A \alpha_A) \circ f \circ (\gamma_A \alpha_A) = (\gamma_B \alpha_B) \circ f \circ (\gamma_B \alpha_B)$$

Main Technical Result

If $f \circ (\gamma_A \alpha_A)$ is continuous then $K_f(A)$ exists and
$$K_f(A) = \text{img}(f^A) \cup \bigcup_{y \in \text{img}(f^A)} \max(\{x \in A \mid f^A(x) = y\})$$

Proof relies on the notion of **complete abstract interpretation**

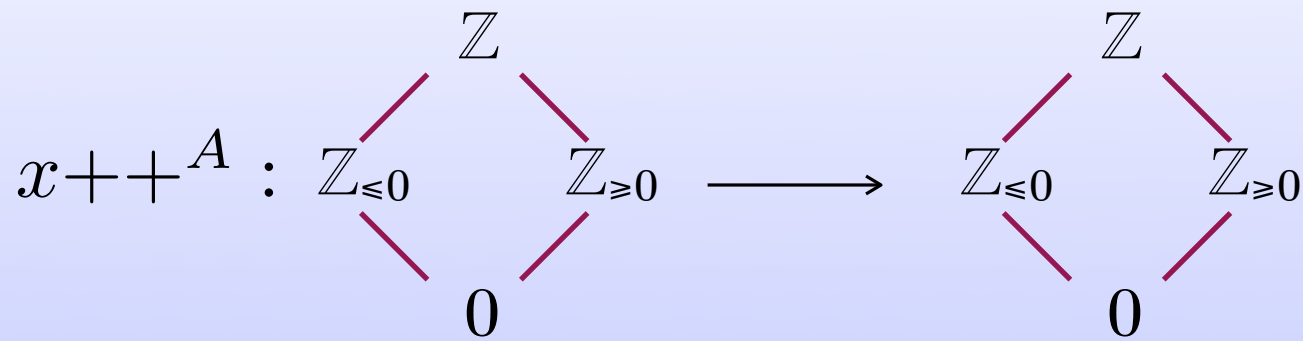
Example



$$\begin{aligned} 0_{++} &= \mathbb{Z}_{\geq 0} \\ \mathbb{Z}_{\leq 0}_{++} &= \mathbb{Z} \\ \mathbb{Z}_{\geq 0}_{++} &= \mathbb{Z}_{\geq 0} \\ \mathbb{Z}_{++} &= \mathbb{Z} \end{aligned}$$

$$K_f(A) = \text{img}(f^A) \cup \bigcup_{y \in \text{img}(f^A)} \max(\{x \in A \mid f^A(x) = y\})$$

Example



$$\begin{aligned} 0 \text{++} &= \mathbb{Z}_{\geq 0} \\ \mathbb{Z}_{\leq 0} \text{++} &= \mathbb{Z} \\ \mathbb{Z}_{\geq 0} \text{++} &= \mathbb{Z}_{\geq 0} \\ \mathbb{Z} \text{++} &= \mathbb{Z} \end{aligned}$$

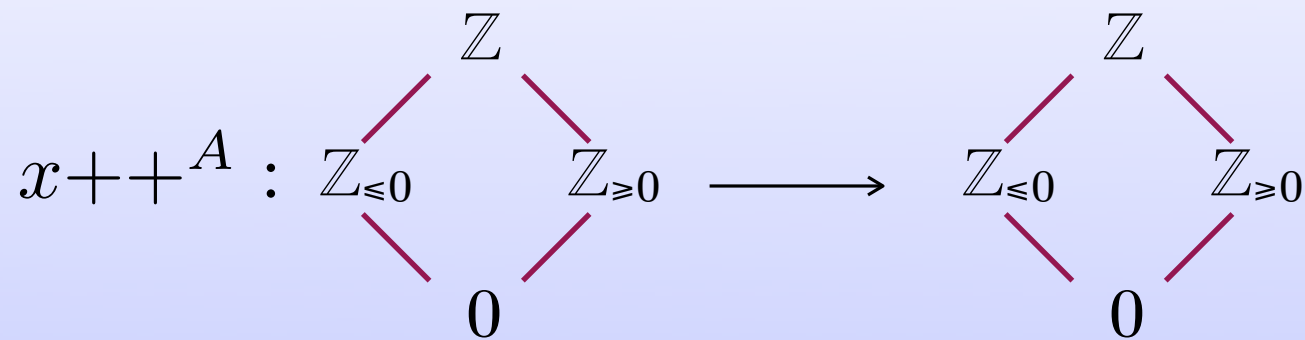
$$K_f(A) = \text{img}(f^A) \cup \bigcup_{y \in \text{img}(f^A)} \max(\{x \in A \mid f^A(x) = y\})$$

$$\text{img}(\text{++}^A) = \{ \mathbb{Z}, \mathbb{Z}_{\geq 0} \}$$

$$\max(\{x \in A \mid \text{++}^A(x) = \mathbb{Z}\}) = \max(\{\mathbb{Z}_{\leq 0}, \mathbb{Z}\}) = \mathbb{Z}$$

$$\max(\{x \in A \mid \text{++}^A(x) = \mathbb{Z}_{\geq 0}\}) = \max(\{0, \mathbb{Z}_{\geq 0}\}) = \mathbb{Z}_{\geq 0}$$

Example



$$\begin{aligned} 0 \text{++} &= \mathbb{Z}_{\geq 0} \\ \mathbb{Z}_{\leq 0} \text{++} &= \mathbb{Z} \\ \mathbb{Z}_{\geq 0} \text{++} &= \mathbb{Z}_{\geq 0} \\ \mathbb{Z} \text{++} &= \mathbb{Z} \end{aligned}$$

$$K_f(A) = \text{img}(f^A) \cup \bigcup_{y \in \text{img}(f^A)} \max(\{x \in A \mid f^A(x) = y\})$$

$$\text{img}(\text{++}^A) = \{ \mathbb{Z}, \mathbb{Z}_{\geq 0} \}$$

$$\max(\{x \in A \mid \text{++}^A(x) = \mathbb{Z}\}) = \max(\{\mathbb{Z}_{\leq 0}, \mathbb{Z}\}) = \mathbb{Z}$$

$$\max(\{x \in A \mid \text{++}^A(x) = \mathbb{Z}_{\geq 0}\}) = \max(\{0, \mathbb{Z}_{\geq 0}\}) = \mathbb{Z}_{\geq 0}$$

$$K_{\text{++}}(A) = \{ \mathbb{Z}, \mathbb{Z}_{\geq 0} \}$$

Abstract Model Checking

Concrete Kripke structure $\langle \Sigma, \rightarrow, \ell \rangle$

Abstract Model Checking

Concrete Kripke structure $\langle \Sigma, \rightarrow, \ell \rangle$

Abstract state space P is a partition of Σ

Abstract Kripke structure $\langle P, \rightarrow^{\exists\exists}, \ell \rangle$

$B \rightarrow^{\exists\exists} C$ iff there exist $x \in B$ and $y \in C$ s.t. $x \rightarrow y$

Abstract Model Checking

Concrete functions:

predecessor pre: $\wp(\Sigma) \rightarrow \wp(\Sigma)$

successor post: $\wp(\Sigma) \rightarrow \wp(\Sigma)$

Abstract Model Checking

Concrete functions:

predecessor pre: $\wp(\Sigma) \rightarrow \wp(\Sigma)$

successor post: $\wp(\Sigma) \rightarrow \wp(\Sigma)$

Partition P can be viewed as an abstraction of $\wp(\Sigma)$

Abstract Model Checking

Concrete functions:

predecessor pre: $\wp(\Sigma) \rightarrow \wp(\Sigma)$

successor post: $\wp(\Sigma) \rightarrow \wp(\Sigma)$

Partition P can be viewed as an abstraction of $\wp(\Sigma)$

What is the correctness kernel of P for pre and post?

Abstract Model Checking

What is the correctness kernel $K(P)$ of P for pre and post?

Abstract Model Checking

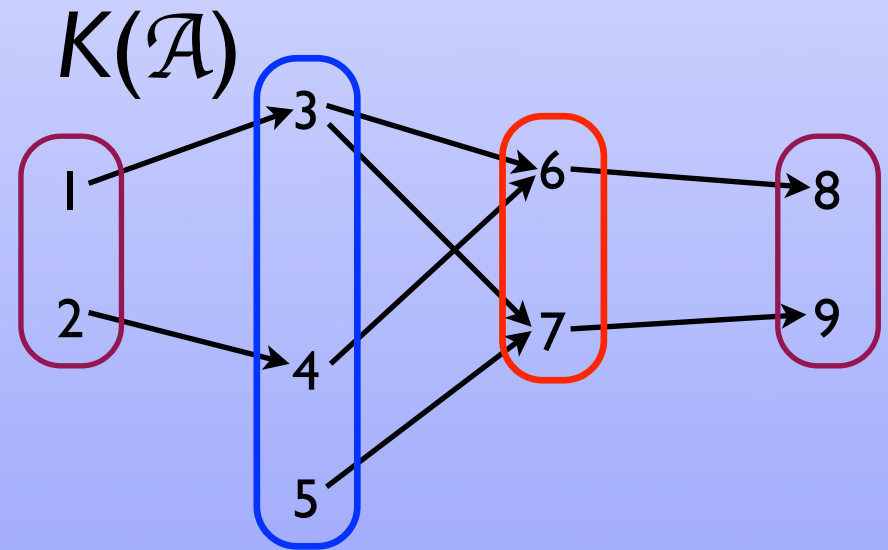
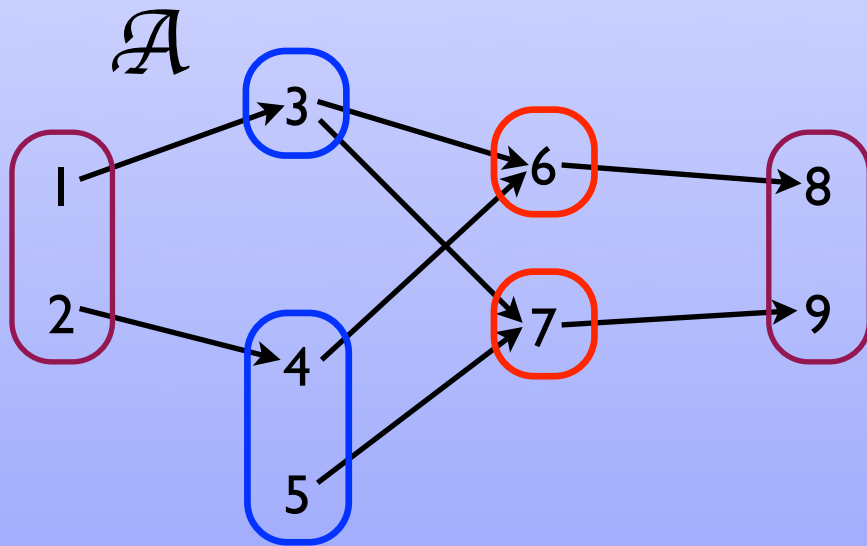
What is the correctness kernel $K(P)$ of P for pre and post?

$K(P)$ merges two blocks B_1 and B_2 iff for any $A \in P$,
 $A \rightarrow^{\exists\exists} B_1 \Leftrightarrow A \rightarrow^{\exists\exists} B_2$ and $B_1 \rightarrow^{\exists\exists} A \Leftrightarrow B_2 \rightarrow^{\exists\exists} A$

Abstract Model Checking

What is the correctness kernel $K(P)$ of P for pre and post?

$K(P)$ merges two blocks B_1 and B_2 iff for any $A \in P$,
 $A \rightarrow^{\exists\exists} B_1 \Leftrightarrow A \rightarrow^{\exists\exists} B_2$ and $B_1 \rightarrow^{\exists\exists} A \Leftrightarrow B_2 \rightarrow^{\exists\exists} A$



EGAS

EGAS: Example-Guided Abstraction Simplification

EGAS

EGAS: Example-Guided Abstraction Simplification

Abstract Kripke structure $\langle P, \rightarrow^{\exists\exists} \rangle$

Correctness Kernel $\langle K(P), \rightarrow^{\exists\exists} \rangle$

EGAS

EGAS: Example-Guided Abstraction Simplification

Abstract Kripke structure $\langle P, \rightarrow^{\exists\exists} \rangle$

Correctness Kernel $\langle K(P), \rightarrow^{\exists\exists} \rangle$

Correctness kernels do not add spurious paths

if π is a spurious path in $K(P)$ then there exists a spurious path σ in P such that $\alpha(\sigma) = \pi$

CEGAR

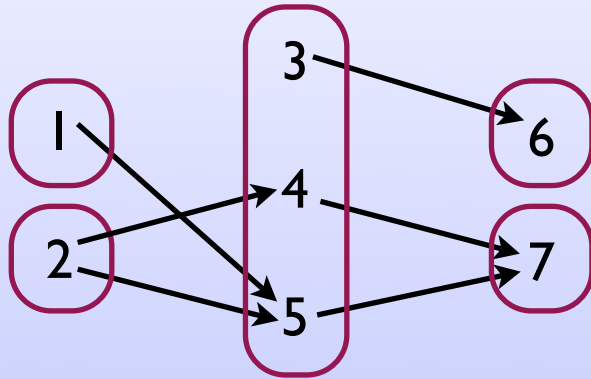
1) Model checker provides an abstract path (i.e. a counterexample)

$$\pi = B_1 \rightarrow^{\exists\exists} B_2 \rightarrow^{\exists\exists} B_3 \dots \rightarrow^{\exists\exists} B_n$$

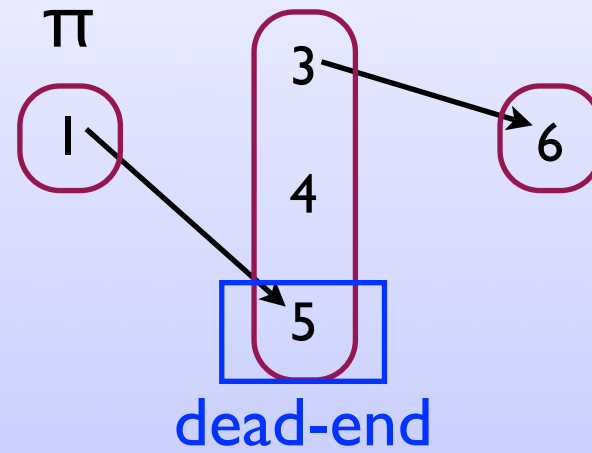
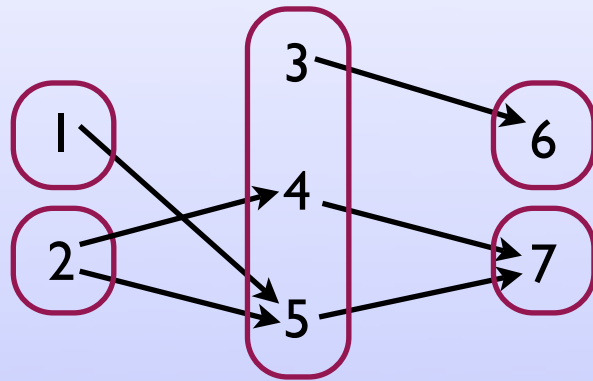
2) CEGAR determines whether π is spurious or not

3) Spuriousness of π depends on some block B_k of π with bad and dead-end states. Thus, CEGAR splits B_k in order to separate bad and dead-end states.

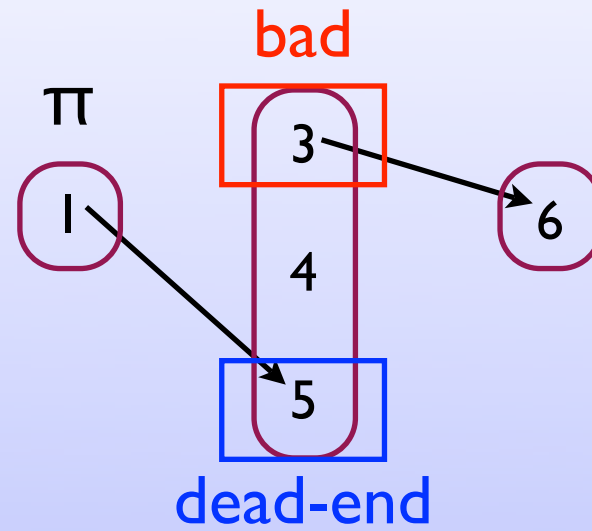
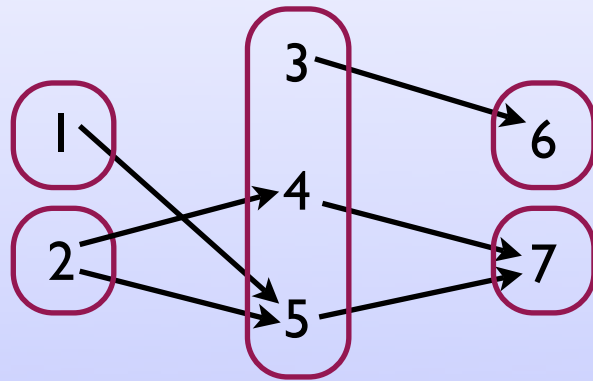
CEGAR



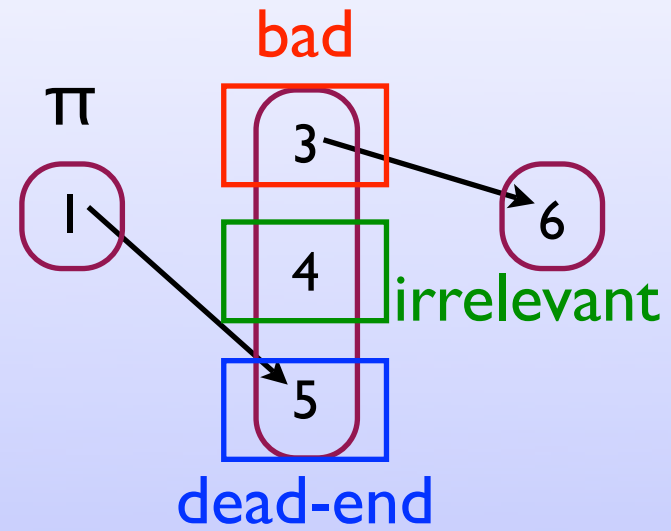
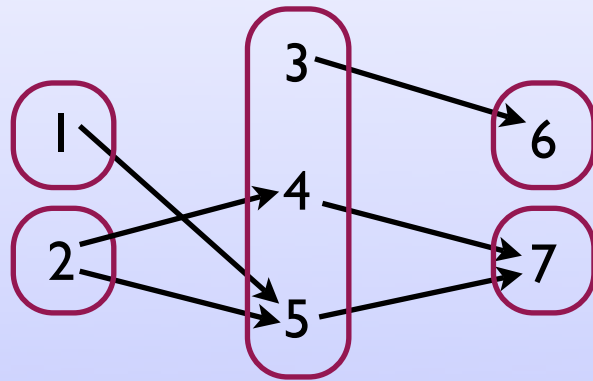
CEGAR



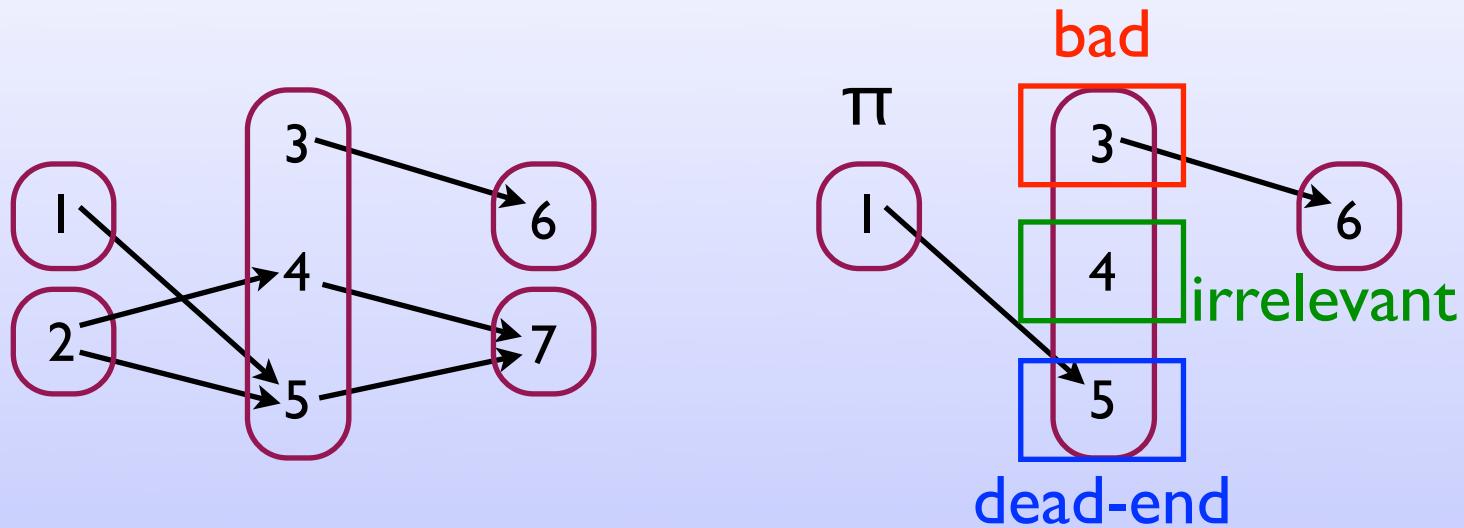
CEGAR



CEGAR



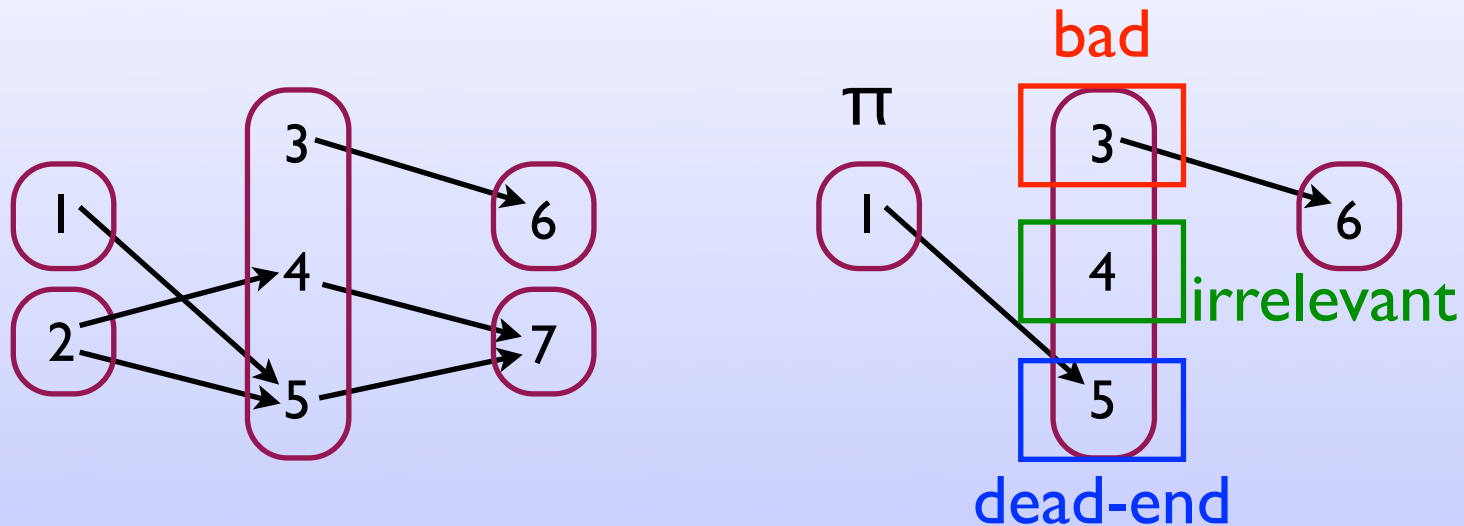
CEGAR



Finding the coarsest refinement is NP-hard

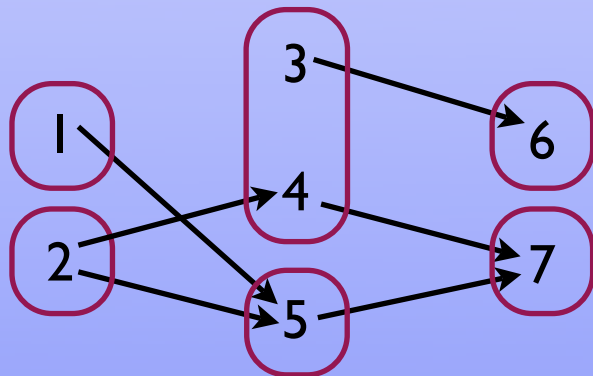
CEGAR heuristics: split into dead-end and bad \cup irrelevant

CEGAR

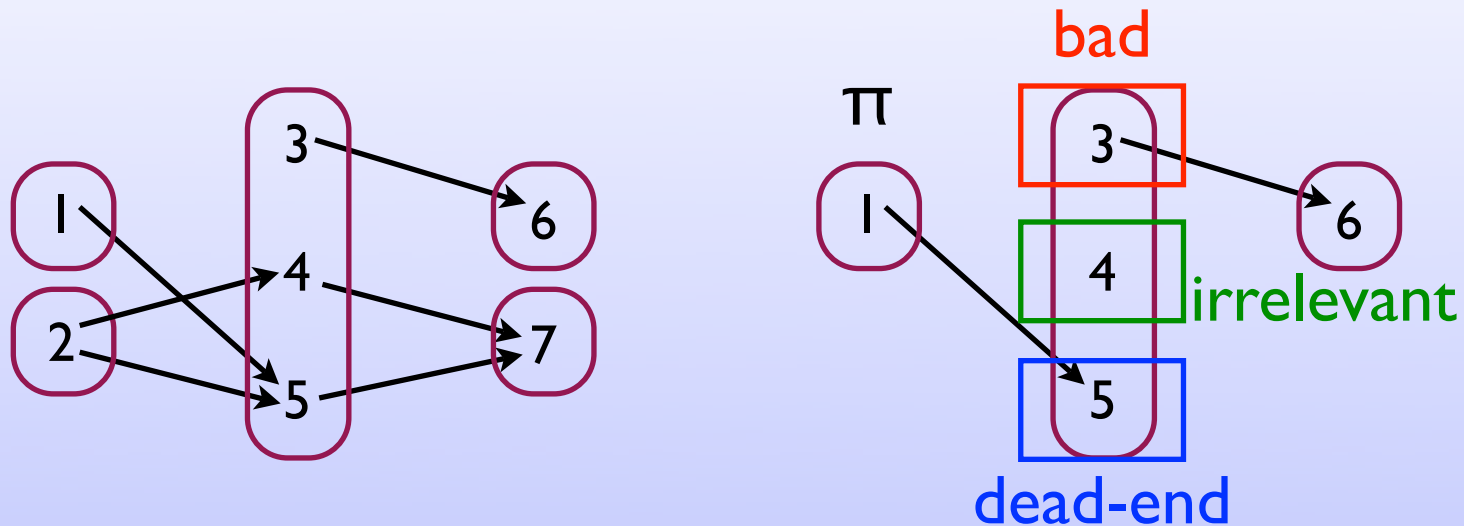


Finding the coarsest refinement is NP-hard

CEGAR heuristics: split into dead-end and bad U irrelevant

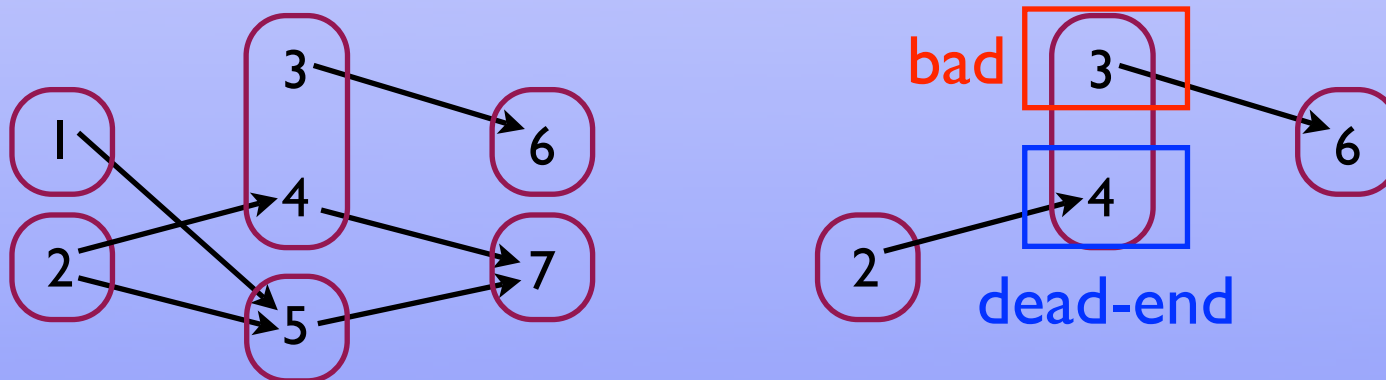


CEGAR

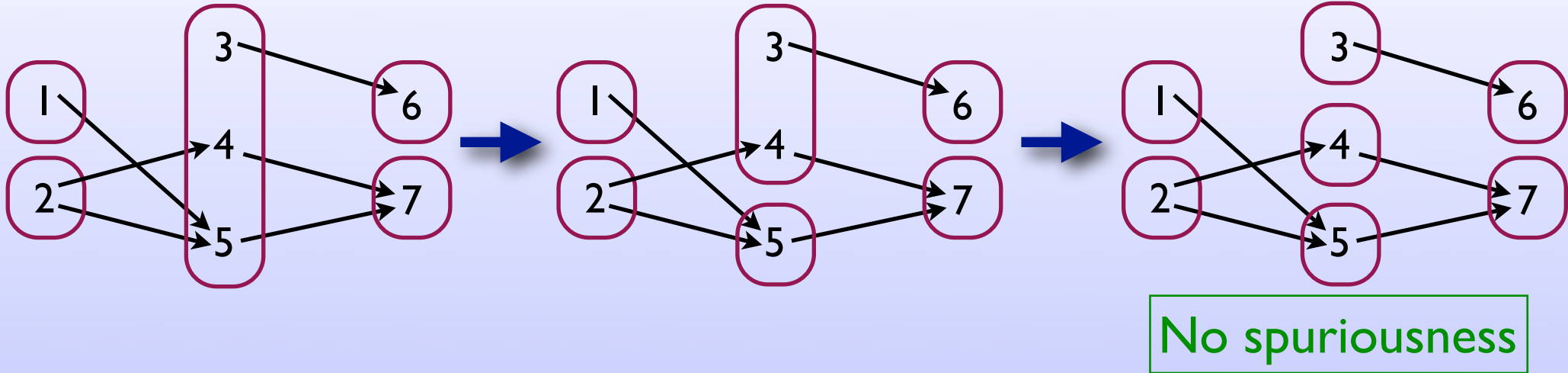


Finding the coarsest refinement is NP-hard

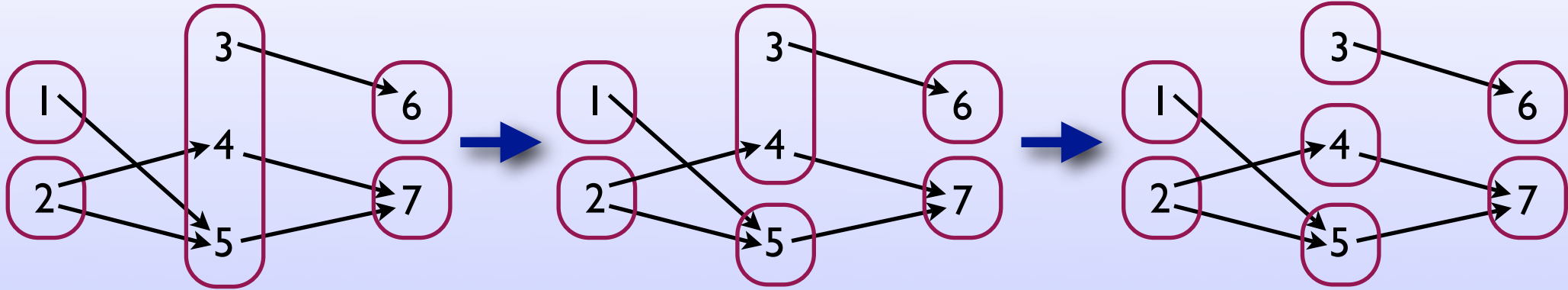
CEGAR heuristics: split into dead-end and bad U irrelevant



CEGAR



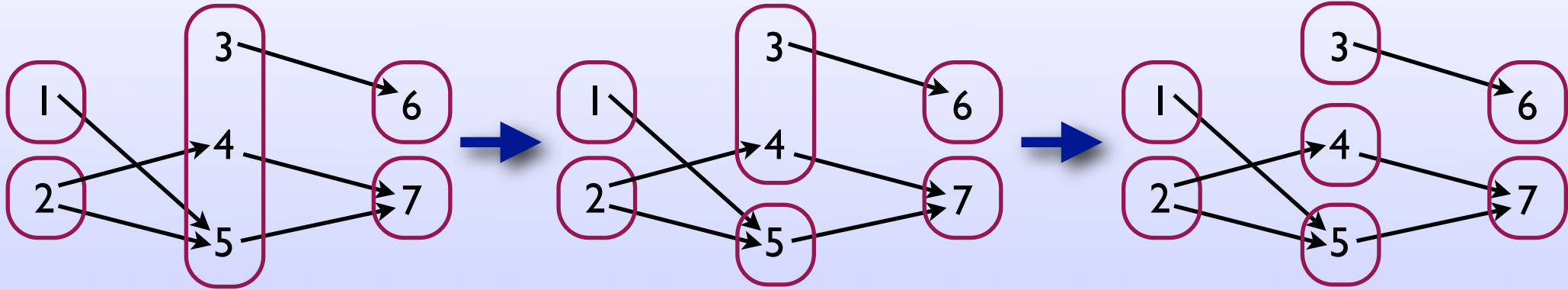
CEGAR



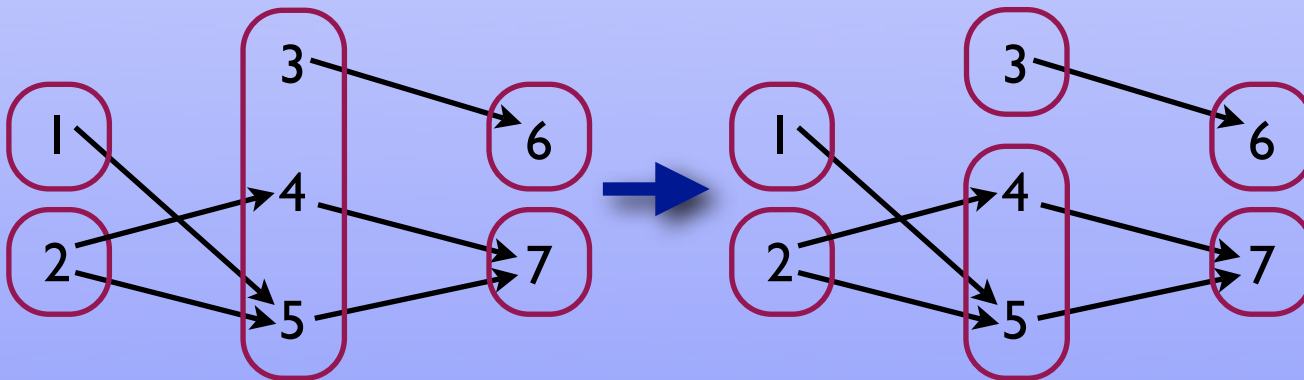
No spuriousness

When irrelevant are joined with dead-end:

CEGAR



When irrelevant are joined with dead-end:



No spuriousness

EGAS and CEGAR

CEGAR heuristics may lead to ineffective abstraction refinements

EGAS and CEGAR

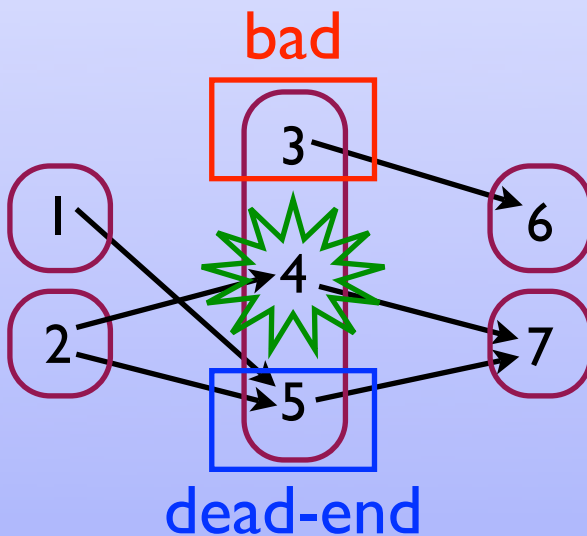
CEGAR heuristics may lead to ineffective abstraction refinements

EGAS suggests a sharper refinement heuristics

EGAS and CEGAR

CEGAR heuristics may lead to ineffective abstraction refinements

EGAS suggests a sharper refinement heuristics



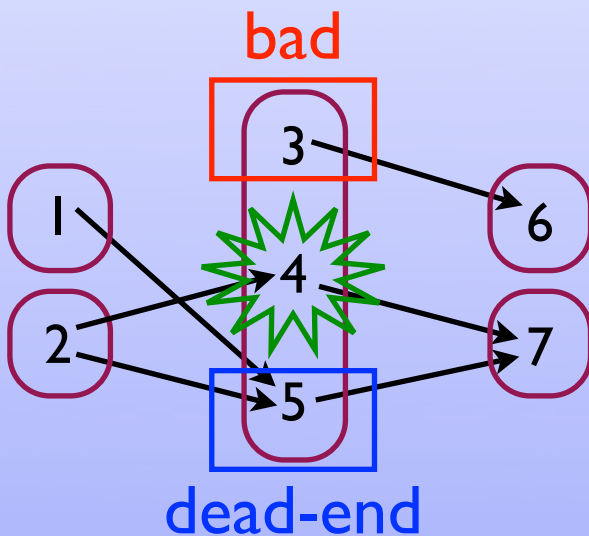
The state irrelevant 4 is **dead-irrelevant**

- 1) can be reached from a block that also reaches a dead-end
- 2) can reach a block that is also reached by a dead-end

EGAS and CEGAR

CEGAR heuristics may lead to ineffective abstraction refinements

EGAS suggests a sharper refinement heuristics



The state irrelevant 4 is **dead-irrelevant**

- 1) can be reached from a block that also reaches a dead-end
- 2) can reach a block that is also reached by a dead-end

Thus, by EGAS, merging dead-irrelevant states with dead-end states does not add spurious paths wrt keeping them separate

EGAS Refinement Heuristics

Dead-irrelevant states

- 1) can be reached from a block that also reaches a dead-end
- 2) can reach a block that is also reached by a dead-end

EGAS Refinement Heuristics

Dead-irrelevant states

- 1) can be reached from a block that also reaches a dead-end
- 2) can reach a block that is also reached by a dead-end

Bad-irrelevant states

- 1) can be reached from a block that also reaches a bad
- 2) can reach a block that is also reached by a bad

EGAS Refinement Heuristics

Dead-irrelevant states

- 1) can be reached from a block that also reaches a dead-end
- 2) can reach a block that is also reached by a dead-end

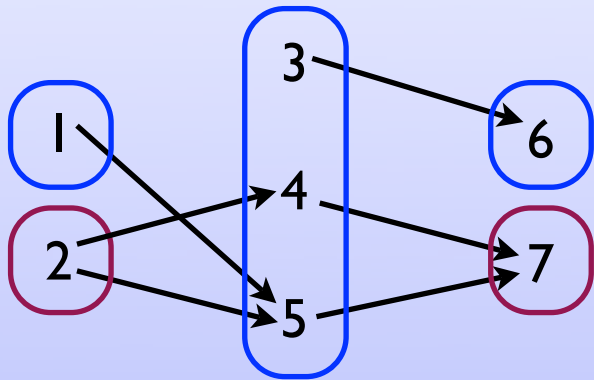
Bad-irrelevant states

- 1) can be reached from a block that also reaches a bad
- 2) can reach a block that is also reached by a bad

Fully-irrelevant states

- 1) neither bad- nor dead-irrelevant OR
- 2) both bad- and dead-irrelevant

EGAS Refinement Heuristics



EGAS Refinement Heuristics



Related Work

Related Work

- ❖ **Core** of an abstract domain [Giacobazzi et al.]
 - ◆ Given an abstract domain property P , this is the most concrete simplification of A that satisfies P

Related Work

- ❖ **Core** of an abstract domain [Giacobazzi et al.]
 - ◆ Given an abstract domain property P , this is the most concrete simplification of A that satisfies P
- ❖ **Compressor** of an abstract domain [Giacobazzi et al.]
 - ◆ Given a refinement Ref , this is the most abstract simplification of A such that: $\text{Ref}(\text{Compressor}(A)) = \text{Ref}(A)$

Conclusions

Conclusions

- ❖ First step in studying abstraction simplifications in static analysis and model checking

Conclusions

- ❖ First step in studying abstraction simplifications in static analysis and model checking
- ❖ Future work
 - ◆ precise relationship between EGAS and CEGAR

Conclusions

- ❖ First step in studying abstraction simplifications in static analysis and model checking
- ❖ Future work
 - ◆ precise relationship between EGAS and CEGAR
 - ◆ integrating EGAS in CEGAR