# Writing Information into DNA

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**Abstract.** The time is approaching when information can be written into DNA. This tutorial work surveys the methods for designing code words using DNA, and proposes a simple code that avoids unwanted hybridization in the presence of shift and concatenation of DNA words and their complements.

# 1 Introduction

As bio- and nano-technology advances, the demand for writing information into DNA increases. Areas of immediate application are:

- DNA computation which attempts to realize biological mathematics, i.e., solving mathematical problems by applying experimental methods in molecular biology [1]. Because a problem must be first encoded in DNA terms, the method of encoding is of crucial importance. Typically, a set of fixed-length oligonucleotides is used to denote logical variables or graph components.
- DNA tag/antitag system which designs fixed-length short oligonucleotide tags for identifying biomolecules (e.g., cDNA), used primarily for monitoring gene expressions [2,3,4].
- DNA data storage which advocates the use of bacterial DNA as a long-lasting high-density data storage, which can also be resistant to radiation [5].
- DNA signature which is important for registering a copyright of engineered bacterial and viral genomes. Steganography (an invisible signature hidden in other information) is useful for the exchange of engineered genomes among developers.

These fields are unlike conventional biotechnologies in that they attempt to *encode artificial information into DNA*. They can be referred to as 'encoding models'. Although various design strategies for DNA sequences have been proposed and some have been demonstrated, no standard code like the ASCII code exists for these models, presumably because data transfer in the form of DNA has not been a topic of research. In addition, requirements for DNA sequences differ for each encoding model.

In this tutorial work, the design of DNA words as information carriers is surveyed and a simple, general code for writing information into biopolymers is

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proposed. After this introduction, Section 2 introduces major constraints considered in the word design. In Section 3, three major design approaches are briefly overviewed and our approach is described in Section 4. Finally, Section 5 shows an exemplary construction of DNA code words using our method.

# 2 Requirements for a DNA Code

DNA sequences consist of four nucleotide bases (A: adenine, C: cytosine, G: guanine, and T: thymine), and are arrayed between chemically distinct terminals known as the 5'- and 3'-end. The double-helix DNA strands are formed by a sequence and its complement. The complementary strand, or *complement*, is obtained by the substitution of base A with base T, and base C with base G and vice versa, and reversing its direction. For example, the sequence 5'-AAGCGCTT-3'is the complement of itself: 5' - AAGCGCTT - 3'is the complement of itself: 5' - AAGCGCTT - 3'a double strand cannot form stable hydrogen bonds and is called a (base) *mismatch*. The stability of a DNA double helix depends on the number and distribution of base mismatches [6].

Now consider a set of DNA words for information interchange. Each word must be as distinct as possible so that no words will induce unwanted hybridization (*mishybridization*) regardless of their arrangement. At the same time, all words must be physico-chemically uniform (*concerted*) to guarantee an unbiased reaction in biological experiments.

In principle, there are two measures for evaluating the quality of designed DNA words: statistical thermodynamics and combinatorics. Although the thermodynamic method may yield a more accurate estimation, its computational cost is high. Therefore, since combinatorial estimations approximate the thermodynamic ones, the focus in this work is on the former method, described in terms of discrete constraints that DNA words should satisfy. In what follows, formal requirements for the DNA word set will be introduced.

#### 2.1 Constraints on Sequences

DNA words are assumed to be of equal length. This assumption holds true in most encoding models. (Some models use oligonucleotides of different lengths for spacer- or marker sequences. As such modifications do not change the nature of the problem, their details are not discussed here.) The design problem posed by DNA words has much in common with the construction of classical errorcorrecting code words.

Let  $x = x_1 x_2 \cdots x_n$  be a DNA word over four bases {A,C,G,T}. The *reverse* of x is denoted  $x^R = x_n x_{n-1} \cdots x_1$ , and the *complement* of x, obtained by replacing base A with T, and base C with G in x and vice versa, is denoted  $x^C$ . The *Hamming distance* H(x, y) between two words  $x = x_1 x_2 \ldots x_n$  and  $y = y_1 y_2 \ldots y_n$  is the number of indices i such that  $x_i \neq y_i$ . For a set of DNA words  $S, S^{RC}$  is its complementation with reverse complement sequences, i.e.,  $\{x \mid x \in S \text{ or } (x^R)^C \in S\}$ .

**Hamming Constraints** As in code theory, designed DNA words should keep a large Hamming distance between all word pairs. What makes the DNA codedesign more complicated than the standard theory of error-correcting code is that we must consider not only H(x, y) but also  $H(x^C, y^R)$  to guarantee the mismatches in the hybridization with other words and their complements (Fig 1).



Fig. 1. Binary Pattern of Hybridization. The complementary strand has a reverse pattern of  $\{A,T\}$  and  $\{G,C\}$  bases. A reverse complement of a DNA word corresponds to its complementary strand.

**Comma-Free Constraints** It is desirable for the designed words to be commafree because DNA has no fixed reading frames. By definition, a code S is commafree if the overlap of any two, not necessarily different, code words  $x_1x_2 \cdots x_n \in S$ and  $y_1y_2 \cdots y_n \in S$ , (i.e.,  $x_{r+1}x_{r+2} \cdots x_ny_1y_2 \cdots y_r$ ; 0 < r < n) does not result in another code word in S [7,8]. The property by which any overlapping word differs from another word in at least d positions is called comma-free with index d. Thus, our DNA code should be comma-free with a high index. <sup>1</sup>

Note that comma-freeness is not replaced by introducing predefined 'spacer' words between code words. Such spacers may facilitate the decoding of words, but they do not contribute to the avoidance of mishybridization. Moreover, spacers lengthen the encoded DNA and lower its information content.

**Energy Constraints** In addition to the above constraints on mismatches, the melting temperatures of DNA words must be very similar to guarantee their concerted behavior *in vitro*. The most reliable estimation is the nearest neighbor approximation, where the temperature is computed from the frequency of 16 base dimers (from AA to TT) [12,6]. Arita and Kobayashi proposed its further approximation by grouping [GC] and [AT], where the temperature depends on the frequency of only 3 patterns ([GC][GC], [GC][AT] or [AT][GC], and [AT][AT]) [13]. Dimer frequency of a sequence x is the three tuple of integers, each describing the frequency of the above 3 patterns in this order. To integrate the terminal

<sup>&</sup>lt;sup>1</sup> The idea of comma-freeness originated in the elucidation of DNA translation mechanism. Early on, DNA codons for 20 amino acids were thought to be encoded in the comma-free manner [9]. Incidentally, the number of comma-free code words of length 3 over 4 bases is at most 20. The systematic design of a comma-free code of index 1 was soon proposed [10,11].

bases, we assume as if x is cyclic in the computation of frequency. For example, AAGCGCTT and TACGGCAT exhibit close melting temperatures because they share the same dimer frequency (3, 2, 3). Thus, all DNA code words should share the same dimer frequency to guarantee their concerted behavior.

**Other Constraints** Depending on the model used, there are constraints in terms of base mismatches. We focus on the first 2 constraints in this paper.

- 1. Forbidden subwords that correspond to restriction sites, simple repeats, or other biological signal sequences, should not appear anywhere in the designed words and their concatenations. This constraint arises when the encoding model uses pre-determined sequences such as genomic DNA or restriction sites for enzymes.
- 2. Any subword of length k should not appear more than once in the designed words. This constraint is imposed to ensure the avoidance of base pair nucleation that leads to mishybridization. The number k is usually  $\geq 6$ .
- 3. A secondary structure that impedes expected hybridization of DNA words should not arise. To find an optimal structure for these words, the minimum free energy of the strand is computed by dynamic programming [14]. However, the requirement here is that the words do not form some structure. This constraint arises when temperature control is important in the encoding models.
- 4. Only three bases, A,C, and T, may be used in the word design. This constraint serves primarily to reduce the number of mismatches by biasing the base composition, and to eliminate G-stacking energy [15]. In RNA word design, this constraint is important because in RNA, both G-C pairs and G-U pairs (equivalent to G-T in DNA) form stably.

### 2.2 Data Storage Style

Because there is no standard DNA code, it may seem premature to discuss methods of aligning words or their storage, i.e., their data-addressing style. However, it is worth noting that the storage style depends on the word design; the immobilization technique, like DNA chips, has been popular partly because its weaker constraint on words alleviates design problems encountered in scaling up experiments.

**Surface-Based Approach** In the surface-based (or solid-phase) approach, DNA words are placed on a solid support (Fig 2). This method has two advantages: (1) since one strand of the double helix is immobilized, code words can be separated (washed out) from their complements, thereby reducing the risk of unexpected aggregation of words [16]; (2) since fluorescent labeling is effective, it is easier to recognize words, e.g., for information readout.



Fig. 2. The Surface-Based versus the Soluble Approach. While they are indistinguishable in solution, immobilization makes it easy to separate information words (gray) from their complements (black).

**Soluble Approach** Easier access to information on surfaces simultaneously limits the innate abilities of biomolecules. DNA fragments in solution acquire more flexibility as information carriers, and have been shown capable of simulating cellular automata [17]. Other advantages of the soluble approach are: (1) it opens the possibility of autonomous information processing [18]; (2) it is possible to introduce DNA words into microbes. The words can also be used for nano structure design.

Any systematic word design that avoids mishybridization should serve both approaches. Therefore, word constraints must extend to complements of code words. Our design problem is then summarized as follows.

**P**roblem: Given two integers l and d (l > d > 0), design a set S of length-l DNA words such that  $S^{RC}$  is comma-free with index d and for any two sequences  $x, y \in S^{RC}$ ,  $H(x, y) \ge d$  and  $H(x^C, y^R) \ge d$ . Moreover, all words in  $S^{RC}$  share the same dimer frequency.

# 3 Previous Works

Due to the different constraints, there is currently no standard method for designing DNA code words. In this section, three basic approaches are introduced: (1) the template-map strategy, (2) De Bruijn construction, and (3) the stochastic method.

#### 3.1 Template-Map Strategy

This simple yet powerful construction was apparently first proposed by Condon's group [16]. Constraints on the DNA code are divided and separately assigned to two binary codes, e.g., one specifies the GC content (called *templates*), the other specifies mismatches between any word pairs (called *maps*). The product of two codes produces a quaternary code with the properties of both codes (Fig 3). Frutos et al. designed 108 words of length 8 where (1) each word has four GCs; (2) each pair of words, including reverse complements, differs in at least four bases [16]. Later, Li et al., who used the Hadamard code, generalized this construction to longer code words that have mismatches equal to or exceeding

half their length [19]. They presented, as an example, the construction of 528 words of length 12 with 6 minimum mismatches.



Fig. 3. Template-Map Strategy. In this figure, templates specify that the sequences contain 50% GCs and four mismatches between them and their complements. Maps are error-correcting code words and specify the choice between A and T, or G and C.

The drawback of this construction is twofold. First, the melting temperatures of the designed quaternary words may differ regardless of their uniform GC content. This property was analyzed in Li et al. and the predicted melting temperatures of the 528 words differed over 20 °C range [19]. The second problem is the comma-freeness. Although the design has been effectively demonstrated in the surface-based approach, scaling up to multiple words will be difficult due to mishybridization.

### 3.2 De Bruijn Construction

The longer a consecutive run of matched base pairs, the higher is the risk of mishybridization. The length-k subword constraint to avoid mishybridization is satisfied with a binary De Bruijn sequence of order k, a circular sequence of length  $2^k$  in which each subword of length k occurs exactly once.<sup>2</sup> A linear time algorithm for the construction of a De Bruijn sequence is known [20]. Ben-Dor et al. showed an optimal choosing algorithm of oligonucleotide tags that satisfy the length-k subword constraint and also share similar melting temperatures [4].

One disadvantage is that the number of mismatches between words may be small, because the length-k constraint guarantees only one mismatch for each k-mer. Another disadvantage is again the comma-freeness.

#### 3.3 Stochastic Method

The stochastic method is the most widely used approach in word design; there are as many types of design software as there are reported experiments.

 $<sup>^2</sup>$  De Bruijn sequence can be quaternary. By using the binary version, however, we can easily satisfy the constraint that the subword does not occur in the complementary strand.

Deaton et al. used genetic algorithms to find code words of similar melting temperatures that satisfy the 'extended' Hamming constraint, i.e., a constraint where mismatches in the case of shift are also considered [21]. (The constraint they named the H-measure, is different from comma-freeness in that it considers mismatches between two words, not their overlaps.) Due to the complexity of the problem, they reported that genetic algorithms can be applied to code words of up to length 25 [22].

Landweber et al. used a random word-generation program to design two sets of 10 words of length 15 that satisfy the conditions (1) no more than five matches over a 20-nucleotide window in any concatenation between all  $2^{10}$  combinations; (2) similar melting temperatures of 45 °C; (3) avoidance of secondary structures; and (4) no consecutive matches of more than 7 base pairs. <sup>3</sup> All of the strong constraints could be satisfied with only 3 bases [15]. Other groups that employed three-base words likewise used random word-generation for their word design [24,23].

Although no detailed analyses for such algorithms are available, the power of stochastic search is evident in the work of Tulpan et al., who could increase the number of code words designed by the template-map strategy [25]. However, they reported that the stochastic search failed to outperform the template-map strategy if searches were started from scratch. Therefore it is preferable to apply the stochastic method to enlarge already designed word sets.

### 4 Methods

### 4.1 Comma-Free Error-Correcting DNA Code

Among the different constraints on DNA code words, the most difficult to satisfy is comma-freeness; no systematic construction is known for a comma-free code of high index. The stochastic search is also not applicable because its computational cost is too high.

The comma-free property is, however, a necessary condition for the design of a general-purpose DNA code. This section presents the construction method for a comma-free error-correcting DNA code, and proposes a DNA code: 112 words of length 12 that mismatch at at least 4 positions in any mishybridization, share no more than 6 consecutive subsequences, and retain similar melting temperatures.

**Basic Design** For this design, we employed the method of Arita and Kobayashi [13]. It can systematically generate a set of words of length  $\ell$  such that any of its members will have approximately  $\ell/3$  mismatches with other words, their complements, and overlaps of their concatenations. They constructed sequences as a product of two types of binary words as in the template-map strategy, except that they used a single binary word, denoted T, as the template. Template T is

<sup>&</sup>lt;sup>3</sup> The fourth condition is unnecessary if the first one is satisfied; presented here are all conditions considered in the original paper.

chosen so that its alignment with subsequent patterns always contains equal to or more than d mismatches.

$$T^{R} TT^{R} T^{R} T^{R} T TT T^{R} T^{R}$$

$$\tag{1}$$

The template specifies the GC positions of the designed words: [GC] corresponds to either 1's or 0's in the template. Since the pattern  $T^R$  specifies the AT/GC pattern of reverse complements, the mismatches between T and  $T^R$ guarantee the base mismatches between forward strands and reverse strands of designed DNAs. Other patterns from TT to  $T^R T^R$  are responsible for shifted patterns.

For the map words, any binary error-correcting code of minimum distance d or greater is used. Then, any pair of words in the resulting quaternary code induces at least d mismatches without block shift because of the error-correcting code, and with block shift or reversal because of the chosen template.

Comma-freeness is not the only advantage of their method. Because a single template is used to specify GC positions for all words, the GC arrangement of resulting code words is uniform, resulting in similar melting temperatures for all words in the nearest neighbor approximation [13].

**Other Constraints** In this subsection, methods to satisfy other practical constraints are introduced.

#### Forbidden subword

Since the error-correcting property of the map words is invariant under exchanging and 0-1 flipping columns of all words, this constraint can be easily satisfied.

# Length-k subword

For the DNA words to satisfy this constraint, two additional conditions are necessary: First, the template should not share any length-k subword with patterns in (1). Second, the map words should not share any length-k subword among them.

The first condition can be imposed when the template is selected. To satisfy the second condition, the obvious transformation from word selection to the Max Clique Problem is used: the nodes correspond to the words, and the edges are linked only when two words do not share any length-k subword (without block shift). Note that the clique size is upper bounded by  $2^k$ .

#### Secondary structure

Since all words are derived from the same template, in the absence of shifts, the number of mismatches can be the minimum distance of the error-correcting code words. Hybridization is therefore more likely to proceed without shifts. To avoid secondary structures, the minimum distance of the error-correcting code words is kept sufficiently large and base mismatches are as much distributed as possible. The latter constraint is already achieved by imposing the length-k subword constraint.

## 5 Results

### 5.1 DNA Code for the English Alphabet

Consider the design for the English alphabet using DNA. For each letter, one DNA word is required. One short error-correcting code is the nonlinear (12,144,4) code [26]. <sup>4</sup> Using a Max Clique Problem solver <sup>5</sup>, 32, 56, and 104 words could be chosen that satisfied the length-6, -7, -8 subword constraint, respectively.

There are 74 template words of length 12 and of minimum distance 4; they are shown in the Appendix. Since 128 words cannot be derived from a single template under the subword constraint, two words, say S and T, were selected from the 74 templates such that both S and T induce more than 3 mismatches with any concatenation of 4 words  $T, S, T^R$ , and  $S^R$  (16 patterns), and each chosen word shares no more than length-5, -6, or -7 subword with the other and with their concatenations. Under the length-6 subword constraint, no template pair could satisfy all constraints. Under the length-7, and -8 subword constraints, 8 pairs were selected. (See the Appendix.) All pairs had the common dimer frequency. Under this condition, DNA words derived from these templates can be shown to share close melting temperatures.

Thus, we found 2 templates could be used simultaneously in the design of length-12 words. There were 8 candidate pairs. By combining one of 8 pairs with the 56 words in the Appendix, 112 words were obtained that satisfied the following conditions:

- They mismatched in at least 4 positions between any pair of words and their complements.
- The 4 mismatch was guaranteed under any shift and concatenation with themselves and their complements (comma-freeness of index 4).
- None shared a subword of length 7 or longer under any shift and concatenation.
- All words had close melting temperatures in the nearest neighbor approximation.
- Because all words were derived from only two templates, the occurrence of specific subsequences could be easily located. In addition, the avoidance of specific subsequences was also easy.

We consider that the 112 words serve as the standard code for the English alphabet. The number of words, 112, falls short of the 128 ASCII characters. However, some characters are usually unused. For example, HTML characters from &#14 to &#31 are not used. Therefore, the 112 words suffice for the DNA ASCII code. This is preferable to loosening the constraints to obtain 128 words.

<sup>&</sup>lt;sup>4</sup> The notation (12,144,4) reads 'a length-12 code of 144 words with the minimum distance 4' (one error-correcting).

<sup>&</sup>lt;sup>5</sup> http://rtm.science.unitn.it/intertools/

#### 5.2 Discussion

The current status of information-encoding models was reviewed and the necessity and difficulty of constructing comma-free DNA code words was discussed. The proposed design method can provide 112 DNA words of length 12 and comma-free index 4. This result is superior to the current standard because it is the only work that considers arbitrary concatenation among words including their complementary strands.

In analyzing the encoding models, error and efficiency must be clearly distinguished. Error refers to the impairment of encoded information due to experimental missteps such as unexpected polymerization or excision. Efficiency refers to the processing speed, not the accuracy, of experiments.

Viewed in this light, the proposed DNA code effectively minimizes errors: First, the unexpected polymerization does not occur because all words satisfy the length-7 subword constraint. <sup>6</sup> Second, the site of possible excision under the application of enzymes is easily identified. Lastly, all words have uniform physico-chemical properties and their interaction is expected to be in concert. The efficiency, on the other hand, remains to be improved. It can be argued that 4 mismatches for words of length 12 are insufficient for avoiding unexpected secondary structures. Indispensable laboratory experiments are underway and confirmation of the applicability of the code presented here to any of the encoding models is awaited.

Regarding code size, it is likely that the number of words can be increased by a stochastic search.

Without systematic construction, however, the resulting code loses one good property, i.e., the easy location of specific subsequences under any concatenation.

The error-correcting comma-free property of the current DNA words opens a way to new biotechnologies. Important challenges include: 1. The design of a comma-free quaternary code of high indices; 2. Analysis of the distribution of mismatches in error-correcting code words; and 3. The development of criteria to avoid the formation of secondary structures.

Also important is the development of an experimental means to realize 'DNA signature'. Its presence may forestall and resolve lawsuits on the copyright of engineered genomes. Currently when a DNA message is introduced into a genome, no convenient method exists for the detection of its presence unless the message sequence is known. In the future, it should be possible to include English messages, not ACGTs, on the input window of DNA synthesizers.

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<sup>&</sup>lt;sup>6</sup> The minimum length for primers to initiate polymerization is usually considered to be 8.

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# Appendix

110010100000         110001010000 <sup>†</sup> 11000001010         101000000011         101100100000 <sup>†</sup> 101000010001         10001000100 <sup>†</sup> 10010001000 <sup>†</sup> 100100001000         100010000001           100010001000         100010000001 <sup>†</sup> 10000010001         10000010000         10000000000           01000100001         0100010000 <sup>†</sup> 01100001000         0100010000         0100000000           0100100000 <sup>†</sup> 0110000001 <sup>†</sup> 00100100000         01000000000         01000000000           0100100000 <sup>†</sup> 0010000001 <sup>†</sup> 0010010000 <sup>†</sup> 00100000000         00100000000000000           0010010100 <sup>†</sup> 0010000001 <sup>†</sup> 00100000000         0000110000000000000000000000000000000
100010010100         10001000101         10000110001 <sup>†</sup> 100000101001         10000010010         0101000010         0101000010         0101000001         0101000001         0100000000         01000000000         01000000000         01000000000         010000000000         01000000000000         0100000000000000         01000000000000000         0100000000000000000000000000000000000
011010000100         011000110000 <sup>†</sup> 01100001001         0101100000         01010010000         0101000000           01001100000 <sup>†</sup> 0100100001 <sup>†</sup> 0010001000         0100010000 <sup>†</sup> 01000000000 <sup>†</sup> 01000000000 <sup>†</sup> 0100000000000 <sup>†</sup> 00100101000 <sup>†</sup> 00100100001 <sup>†</sup> 00100001000 <sup>†</sup> 00100000000 <sup>†</sup> 00100000000 <sup>†</sup> 00100000000 <sup>†</sup> 0010010100 <sup>†</sup> 00100010101         00100001000 <sup>†</sup> 0000100000 <sup>†</sup> 0000100000 <sup>†</sup> 0000100000 <sup>†</sup> 0001000110         000000000101         00000000000 <sup>†</sup> 00001000000         00001000000000 <sup>†</sup> 0000100000 <sup>†</sup> 00010001110         000000000000 <sup>†</sup> 000000000000 <sup>†</sup> 000000000000 <sup>†</sup> 00000000000 <sup>†</sup> 00000000000 <sup>†</sup> 0111100110         0111110001 <sup>†</sup> 0101111010 <sup>†</sup> 0111011010 <sup>†</sup> 0111011011         011011110 <sup>†</sup> 0110110111         010111101 <sup>†</sup> 1001111101 <sup>†</sup> 0101111011         0101111011 <sup>†</sup> 0101111011 <sup>†</sup> 0110101011         1011101001 <sup>†</sup> 1011101011 <sup>†</sup> 1001111101 <sup>†</sup> 1001111011 <sup>†</sup> 0110101101         1011101011 <sup>†</sup> 1011010111 <sup>†</sup> 1001110111 <sup>†</sup> 10011101011 <sup>†</sup> 1001110101 <sup>†</sup> 1001110
010011000001         01001001001         01000110100         01000100011         01000000011         01000000011           001110010000 <sup>†</sup> 001101000001 <sup>†</sup> 001100000110         00101010000 <sup>†</sup> 001001000011         00100100001 <sup>†</sup> 00101010100 <sup>†</sup> 00100100101         00100001100 <sup>†</sup> 00101000001         0001010000 <sup>†</sup> 001010000011           0001010100 <sup>†</sup> 0001001001 <sup>†</sup> 00010010101         0000110000 <sup>†</sup> 000110000011         000010001001 <sup>†</sup> 00010101010         00000101001 <sup>†</sup> 000001001010 <sup>†</sup> 00001100000         0000110000000000000000000000000000000
001110010000 <sup>†</sup> 001101000011 <sup>†</sup> 00110100010001 <sup>†</sup> 001001010000 <sup>†</sup> 0010010000000000000000000000000000000
001110010000 <sup>†</sup> 001101000011 <sup>†</sup> 00110100010001 <sup>†</sup> 001001010000 <sup>†</sup> 0010010000000000000000000000000000000
001001010100 <sup>†</sup> 001000100101         00100001101 <sup>†</sup> 00011000010         00011000010         0001010000 <sup>†</sup> 000101001010         000010010101 <sup>†</sup> 00010001100         00001100100         00001101000         00001101000           000101001110         00000100111         00000100110 <sup>†</sup> 00110101111         0111101011         00001101111         00001101111           0011011011         01001101111 <sup>†</sup> 0101101111 <sup>†</sup> 01011101101 <sup>†</sup> 0111110111         0111111011           0110111011         0110111111 <sup>†</sup> 0101111101 <sup>†</sup> 0111110111         0111111111         0111111111           0110111111         01101111110 <sup>†</sup> 0111111111 <sup>†</sup> 0111111111         0111111111 <sup>†</sup> 01111111111 <sup>†</sup> 0110111011         0110111111         0111111111 <sup>†</sup> 0111111111         0111111111 <sup>†</sup> 0111111111111 <sup>†</sup> 0110111111         01111111111 <sup>†</sup> 1001111111         1001111111         1011111111 <sup>†</sup> 0110111111         1011111110 <sup>†</sup> 1011111111111111111111111111111111111
000010001110         0000010011         00000100110 <sup>†</sup> 00110101111         00111010111         0011111100           0111111100         01001101111 <sup>†</sup> 01011011011 <sup>†</sup> 01011110110 <sup>†</sup> 01011111100         01101111101 <sup>†</sup> 0111110011         0110111111 <sup>†</sup> 0101111101 <sup>†</sup> 01011111011 <sup>†</sup> 01011111011 <sup>†</sup> 01011111101 <sup>†</sup> 01111100110         01101111100         01110111101 <sup>†</sup> 01011111011         011101111101 <sup>†</sup> 0110111011         1010111101 <sup>†</sup> 10001111101         1001110111 <sup>†</sup> 1001111011 <sup>†</sup> 1010110111         1010110111         1010101111         1001111101         1011100111 <sup>†</sup> 1010101011         101110100 <sup>†</sup> 101111001111         1001111111         1001111011 <sup>†</sup> 1010101011         10111010111         1010011111         10001111111         1001111011 <sup>†</sup> 1010101011         11101001111         1101001111 <sup>†</sup> 1101101010 <sup>†</sup> 1101110011 <sup>†</sup> 1100011101         1110001111         1110100111 <sup>†</sup> 1101101010 <sup>†</sup> 1101101010 <sup>†</sup> 1110001111         1110001110 <sup>†</sup> 1110101010 <sup>†</sup> 1110101010 <sup>†</sup> 1110101010 <sup>†</sup> 11100011011         11110100110 <sup>†</sup> 11101010101 <sup>†</sup>
001111111010         010011011111 <sup>†</sup> 01011011011 <sup>†</sup> 01011110110 <sup>†</sup> 01011111001         01101011011 <sup>†</sup> 011011100111         01101111100         01110011101 <sup>†</sup> 010111101101         011101110101         011101110101           011011100111         01101111100 <sup>†</sup> 10001111101 <sup>†</sup> 10010111011         1001110111         1001110111 <sup>†</sup> 0110111011         1011010111         10001111101         1001110111         1001110111         10011101111           1010101011         101110100 <sup>†</sup> 1011110011         10110011111         1001111011         10011101111           1010101011         10111100 <sup>†</sup> 101111001111         10001101111         10011101110 <sup>†</sup> 1001111011110 <sup>†</sup> 1010101011         1101011100 <sup>†</sup> 10111001111         1100101111 <sup>†</sup> 1001111001 <sup>†</sup> 1001111001 <sup>†</sup> 1100101101         1110011100 <sup>†</sup> 1101001111 <sup>†</sup> 11011010101 <sup>†</sup> 1101101010 <sup>†</sup> 1101101010 <sup>†</sup> 1110011101         1110001111 <sup>†</sup> 1101001111 <sup>†</sup> 1101101010 <sup>†</sup> 1101101010 <sup>†</sup> 1101101010 <sup>†</sup> 11100011011         11101001110 <sup>†</sup> 1110100110 <sup>†</sup> 1110101010 <sup>†</sup> 1110101010 <sup>†</sup> 1101100101 <sup>†</sup> 00000000000 <sup>†</sup>
$\begin{array}{cccccccccccccccccccccccccccccccccccc$
011111001101         01111101011 <sup>†</sup> 10001111101 <sup>†</sup> 100101111011         1001110111 <sup>†</sup> 10100110111         10101101011         1010111010         10110011110         10110011110           10100111011         10101101011         1010111010         10110011110         10110011110           1011011001         101111000 <sup>†</sup> 10111100011         11000110111         1001011110         1011001011 <sup>†</sup> 10101010111         11000110101         1101001101         1100101011 <sup>†</sup> 1101101010 <sup>†</sup> 10011110011           1100011011         1110010110         11101001110         1101010101 <sup>†</sup> 1101101010 <sup>†</sup> 1101101001           11100011011         11100001111         1110010101 <sup>†</sup> 1101101010 <sup>†</sup> 1101101001 <sup>†</sup> 11100010011         11110100110 <sup>†</sup> 11101010011 <sup>†</sup> 1110101001 <sup>†</sup> 1110101001 <sup>†</sup> 00000000000 <sup>†</sup> 1111111111 <sup>†</sup> 0000011101 <sup>†</sup> 00000110011 <sup>†</sup> 00010011011 <sup>†</sup> 00010011011 <sup>†</sup> 00001011010 <sup>†</sup> 00100110110 <sup>†</sup> 00100110110 <sup>†</sup> 0011001101 <sup>†</sup> 0011001101 <sup>†</sup> 0000000000 <sup>†</sup> 111101001010 <sup>†</sup> 00100001111 <sup>†</sup> 0010011001 <sup>†</sup> 0011001101 <sup>†</sup> 00010011010 <sup>†</sup>
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$\begin{array}{c} 000000000000^\dagger \ 111111111111^\dagger \ 00000111111 \ 0000111011^\dagger \ 000101100111 \ 0001100111^\dagger \ 000110011011^\dagger \ 000110011011^\dagger \ 0011100011011^\dagger \ 001110001101^\dagger \ 001010011011^\dagger \ 001010011011^\dagger \ 001010001111^\dagger \ 001010011011^\dagger \ 001011001101^\dagger \ 010100001111^\dagger \ 010100001111^\dagger \ 010100001111 \ 0101000001111 \ 01011000001 \ 11111000000 \ 111100010100^\dagger \ 011110100001 \ 111111000000 \ 111100010100^\dagger \ 01110000001 \ 0100000000000000000000$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$
$011000101110  011011001010^{\dagger}  011101011000^{\dagger}  011110100001  111111000000  111100010100^{\dagger}$
$111010011000^{\dagger} \ 111001100100 \ \ 111001000011^{\dagger} \ \ 110110000110 \ \ \ 110101100010 \ \ \ 110101001001 \ \ \ 110101001001 \ \ \ \$
$110011001100 \hspace{0.1cm} 110000111001^{\dagger} \hspace{0.1cm} 101110001010^{\dagger} \hspace{0.1cm} 101101010010^{\dagger} \hspace{0.1cm} 101011110000 \hspace{0.1cm} 101011000101^{\dagger}$
$101000101011  100111101000  100111010001  100100110101^{\dagger}  100010100111^{\dagger}  1000010111110 \\$

(12,144,4) Code. Daggers indicate 56 words that satisfy the length-7-subword constraint.

Templates of Length 12. When their reversals and 01-flips are included, the total number of words is 74.

000110011101 and $001010111100$	000110011101 and $001111010100$
001010111100 and $101110011000$	001111010100 and $101110011000$
010001100111 and $110000101011$	010001100111 and $110101000011$
110000101011 and $111001100010$	110101000011 and $111001100010$

Template Pairs Satisfying Minimum Distance 4 and Length-7-subword Constraint.