



Declaration of Independence (1776)

Declaration of the Rights of Man and of the Citizen (1789)



1977

②

The Declaration of Abstract Interpretation of CC77

A statement of principles of
program analysis:

- compare interpretations
- compose interpretations
- celebrate infinity



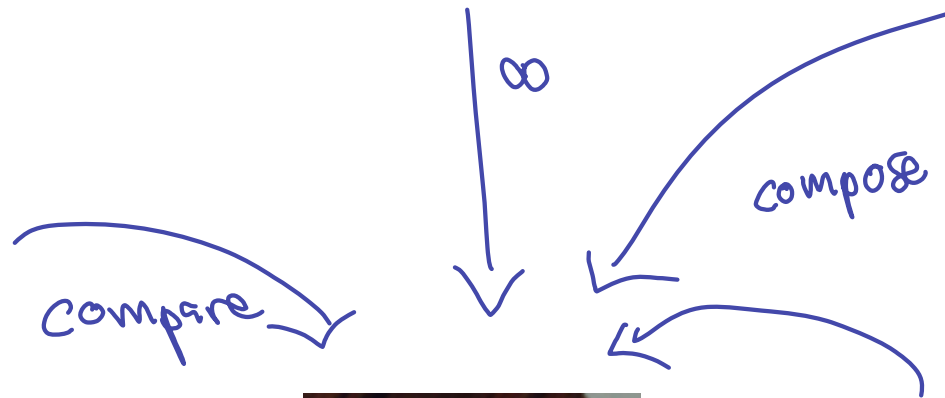
A. Turing



Alfred Tarski (1902-1983)



É. Galois



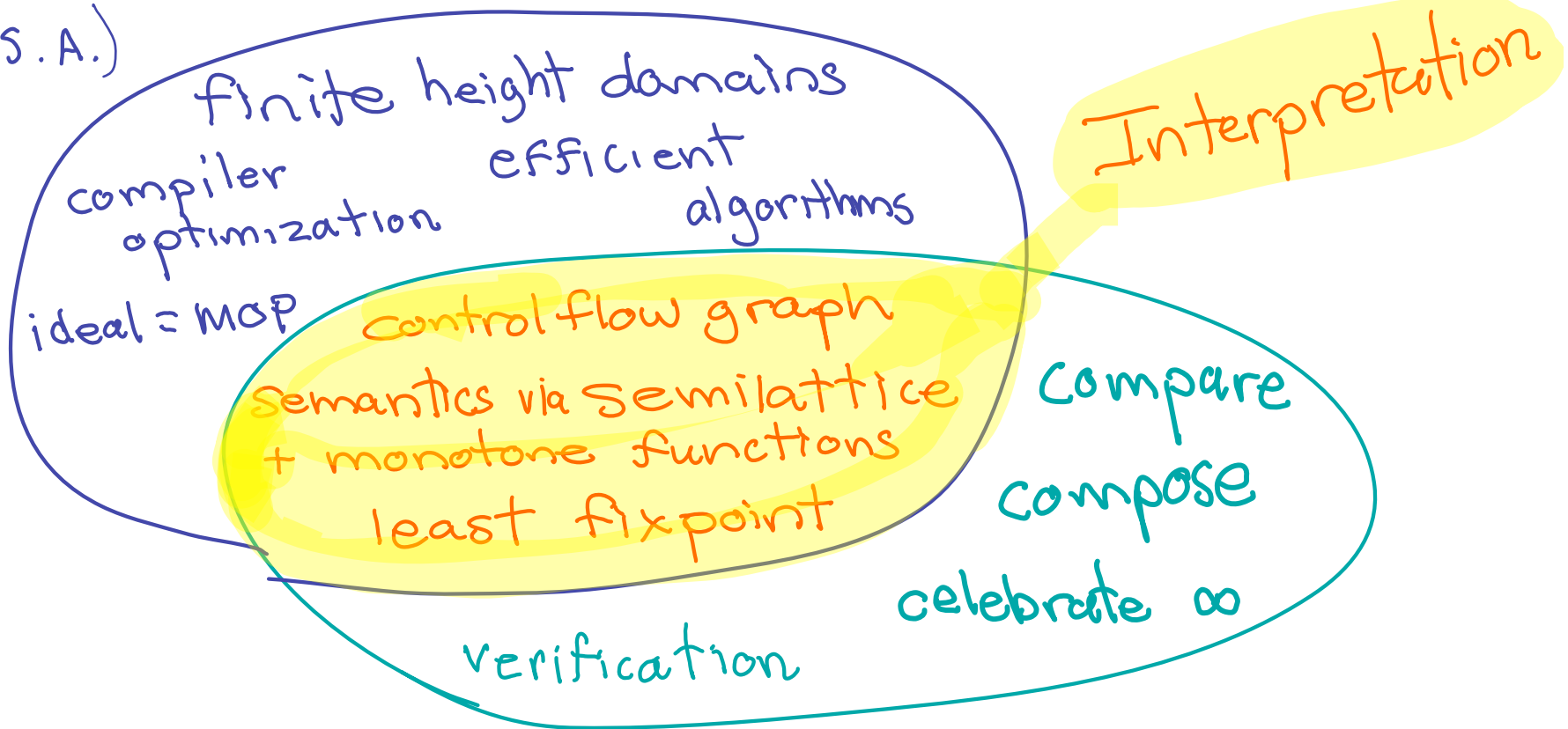
D. Scott



All in the Family (1977)

Dataflow analysis

(U.S.A.)

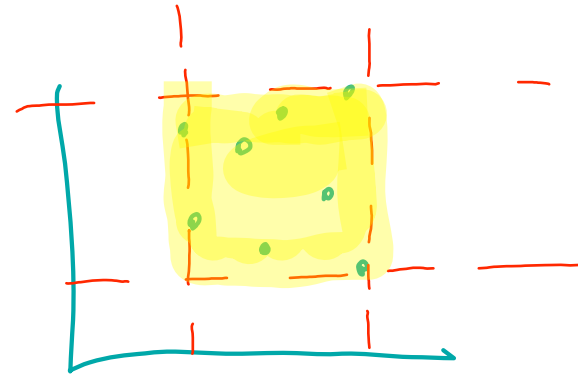


Abstract Interpretation
(France)

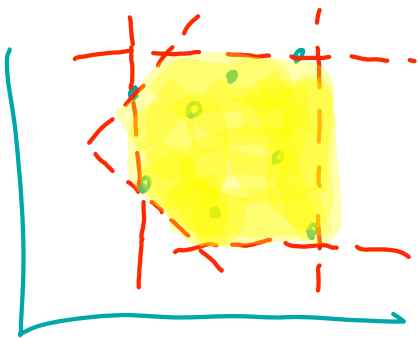
Compare



integer sets

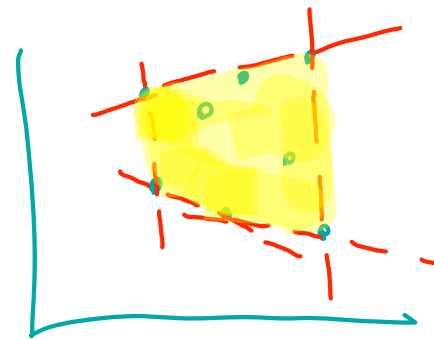


intervals
 $c \leq x < d$



octagon
 $|x| + |y| \leq c$

$$|x| + |y| \leq c$$



polyhedra
 $a_1x_1 + \dots + a_nx_n \leq c$

$$a_1x_1 + \dots + a_nx_n \leq c$$

Diplomacy

webster.2: skill in handling affairs without arousing hostility



Frenchman Charles Maurice de Talleyrand is considered one of the most skilled diplomats of all time

Diplomacy

webster.2: skill in handling affairs without arousing hostility



Frenchman Patrick Cousot
may not be one of the
most skilled diplomats of all time

Patrick's Theme, Take 1

Anything You Can Do, I Can Do Better

Irving Berlin

Anything you can do, I can do better

I can do any thing better than you

No you can't, Yes I can, No you can't, Yes I can

No you can't, Yes I can, yes I can



Patrick's Theme, Take 2

Anything You Can Do, I Can ^{Specify} Do Better

Irving Berlin

Anything you can do, I can specify better

I can specify any thing better than you

No you can't, Yes I can, No you can't, Yes I can

No you can't, Yes I can, yes I can



Compose

Andreas Podelski:

"What abstraction
does SLAM compute?"

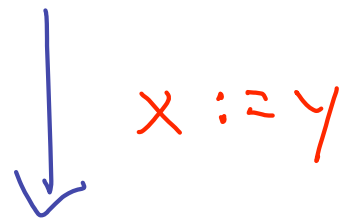
Sriram & Tom:

"Uh... we implemented
c2bp and proved it sound."

Apply Ideal

$$P = \{x > 5, x < 5, y = 5\} \quad x := y$$

$$\delta_{\text{bool}}(\{ \langle 0, 0, 0 \rangle \}) = \{s \mid s \models x = 5 \wedge y \neq 5\}$$



$$\begin{aligned} & \alpha_{\text{bool}}(\{s \mid s \models x = y \wedge y \neq 5\}) \\ &= \{ \langle 1, 0, 0 \rangle, \langle 0, 1, 0 \rangle \} \end{aligned}$$

Apply SLAM

S: $x := y$

S_{BP} : $\{x < 5\}, \{x > 5\}, \{y = 5\} := *, *, \{y = 5\}$

$\{ \langle 0, 0, 0 \rangle \}$

$\downarrow S_{BP}$

$\{ \langle 0, 0, 0 \rangle, \langle 0, 1, 0 \rangle, \langle 1, 0, 0 \rangle, \langle 1, 1, 0 \rangle \}$

Cartesian Abstraction

Approximate a set of tuples
by a tuple of sets

$$\alpha_{\text{cart}}(\{ \langle 1, 0, 0 \rangle, \langle 0, 1, 0 \rangle \}) = \langle *, *, 0 \rangle$$

$$\gamma_{\text{cart}}(\langle *, *, 0 \rangle) = \{ \langle 0, 0, 0 \rangle, \langle 0, 1, 0 \rangle, \langle 1, 0, 0 \rangle, \langle 1, 1, 0 \rangle \}$$

SLAM Abstraction

Not

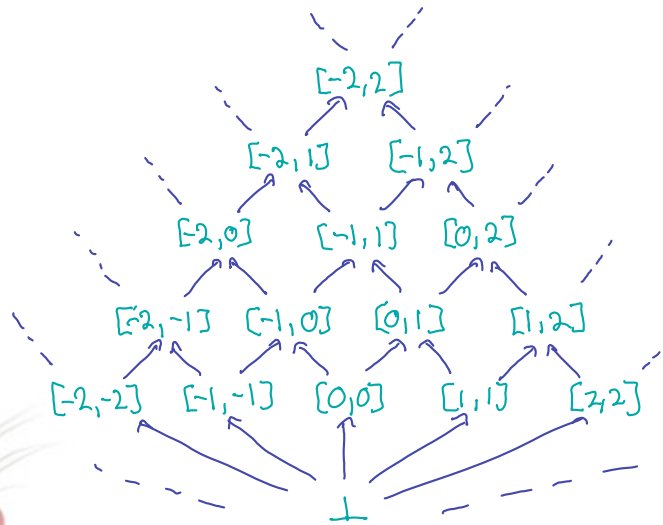
$$\alpha_{\text{bool}} \circ \text{SP} \circ \gamma_{\text{bool}}$$

Rather

$$\alpha_{\text{cart}} \circ \alpha_{\text{bool}} \circ \text{SP} \circ \gamma_{\text{bool}} \circ \gamma_{\text{cart}}$$

Celebrate ∞ !

The chef
has an ∞ lattice!



A recipe for tasty
abstractions!



Cousot, Halbwachs (1978)

Discovering linear equalities

- Wegbreit '75, Karr '76
- required finite ascending chains

Discovering linear inequalities, CH78

- convex polyhedra
- infinite ascending chains

$$(x=1) (1 \leq x \leq 2) \dots (1 \leq x \leq n) \dots$$

- widening, narrowing

Impact

Theory (precision, fixpoint with ∞ domains)
CC 77, ...

Algorithms, Data structures
CH 78, ...

Application

..., ASTREE, ...

Software Tools from Microsoft (2007)

- Windows device drivers
 - Static Driver Verifier (SLAM)
 - part of Windows Vista DDK
- Buffer overflow checking for C/C++
 - SAL + ESPx
 - 1000s of defects fixed
- .NET (managed) code
 - Clousot checker

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Abstract Interpretation

Abstract
Interpretation

