

# Artificial Intelligence: Second Partial test

04 June 2018

## 1 Exercise 1 (Points 30)

Consider an undiscounted MDP having three states (1,2,3). State 3 is terminal. In state 1 and 2 there are two possible actions  $A$  and  $B$ . The transition and reward models are as follow:

- In state 1, action  $A$  moves the agent to state 2 with probability .8 and a reward of  $-2$  while it leaves the agent in state 1 with probability .2 and a reward of  $-1$ . In state 1, action  $B$  moves the agent to state 3 with probability .8 and a reward of 0 while it leaves the agent in state 1 with probability .2 and a reward of  $-1$ .
- In state 2, action  $A$  moves the agent to state 1 with probability .8 and a reward of  $-1$  while it leaves the agent in state 2 with probability .2 and a reward of  $-2$ . In state 2, action  $B$  moves the agent to state 3 with probability .8 and a reward of 0 while it leaves the agent in state 2 with probability .2 and a reward of  $-2$ .

Answer the following questions:

1. Provide a transition diagram for the MDP described above.
2. Provide a qualitative discussion about the optimal policy for this MDP.
3. Show the value of  $v(1)$  for the first two iterations of a Value Iteration algorithm. Assume  $v(s) = 0 \forall s$ .
4. Is it necessary to compute the value of  $v(2)$  to answer to the previous question ? Motivate your answer.

## 2 Exercise 2 (Points 30)

Consider the Bayesian Network in Figure 1. Answer the following questions:

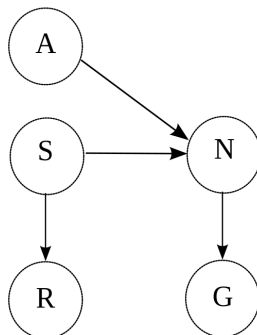


Figure 1: Bayesian Network.

1. State whether we can guarantee that  $N$  is conditionally independent from  $R$  given  $(S, A)$ . Motivate your answer.
2. State whether we can guarantee that  $A$  is conditionally independent from  $G$  given  $S$ . Motivate your answer.
3. Assume variables  $\{S, N\}$  can take three different values while  $\{A, R, G\}$  are binary. State how many parameters must be provided to compute the joint probability table for this Bayesian Network.

### 3 Exercise 3 (Points 30)

Consider an environment with states  $\{A, B, L, R\}$ , actions  $\{r, l\}$  where states  $\{L, R\}$  are terminal. Assume  $\gamma = 1$  and  $\alpha = 0.5$ . Consider the following sequence of learning episodes:

E1  $(A, r, B, 0)(B, r, R, +1)$

E2  $(A, r, B, 0)(B, l, A, 0)$

E3  $(A, r, B, 0)(B, l, R, +1)$

1. Build an estimate for  $\hat{T}$  and  $\hat{R}$
2. Compute  $v(s)$  for all non-terminal states by using a direct evaluation approach
3. Compute  $v(s)$  for all non-terminal states by using a sample-based evaluation approach