

Automated Reasoning  
Written test  
12 February 2010 (I Session)

**1 Exercise 1 (10)**

Decide, using DPLL, whether the following set of clauses are satisfiable, and if they are, provide a model

1.  $\neg a \vee \neg b \vee x, \neg x \vee a, \neg x \vee b, \neg x \vee z, \neg b \vee z, \neg z \vee x \vee b$
2.  $p \vee q, \neg p \vee \neg q, p \vee s, \neg p \vee \neg s, q \vee s, \neg q \vee \neg s$

**2 Exercise 2 (20)**

Prove the unsatisfiability of the following set of ordered clauses by Linear Ordered Resolution

1.  $\neg D(x) \vee P(x)$
2.  $\neg L(x, y) \vee \neg C(y) \vee D(x)$
3.  $L(x, y) \vee D(x)$
4.  $C(a)$
5.  $\neg P(x)$

Use the last clause as top clause.

**3 Exercise 3 (18)**

Given the constraint network  $\mathcal{N}$ :

- Variables:  $\{X, Y, Z, W\}$ , Domain  $D_x = D_y = D_z = \{0, 1\}$  and  $D_w = \{0, 1, 2\}$
- Constraints:  $X > Y, X < W, X < Z, Y = Z$

describe an execution of AC-3. Is the resulting network arc consistent? Is the resulting network consistent? Motivate your answers.

## 4 Exercise 4 (20)

Given the soft graph coloring problem below, apply the Branch and Bound algorithm to find an optimal solution. Use ordering  $d = \{x_1, x_2, x_3, x_4\}$ .

- Variables:  $\{x_1, x_2, x_3, x_4\}$ , Domain  $D_i = \{0, 1\}$
- Constraints:  $R_{12}, R_{13}, R_{23}, R_{24}$
- $F_{ij} : \{ \langle (1, 1), -1 \rangle, \langle (0, 1), 0 \rangle, \langle (1, 0), 0 \rangle, \langle (0, 0), -2 \rangle \}$

## 5 Exercise 5 (32)

Given a combinatorial auction and the following set of bids:

- $B_1 = \langle \{1, 2, 3\}, 5 \rangle$ ,  $B_2 = \langle \{1, 4, 6\}, 4 \rangle$ ,  $B_3 = \langle \{4, 5\}, 1 \rangle$ ,  $B_4 = \langle \{2, 5\}, 3 \rangle$

Answer to the following questions:

1. Provide a cost network formalisation of the winner determination problem, specifying the variables, their domain and the constraints (hard and soft).
2. Is the resulting cost network acyclic ? Motivate your answer
3. Solve the cost network with a solution technique of your choice.